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Economic Analysis of ALFALFA YIELD RESPONSE to PHOSPHATE FERTILIZER at Three Locations in the West

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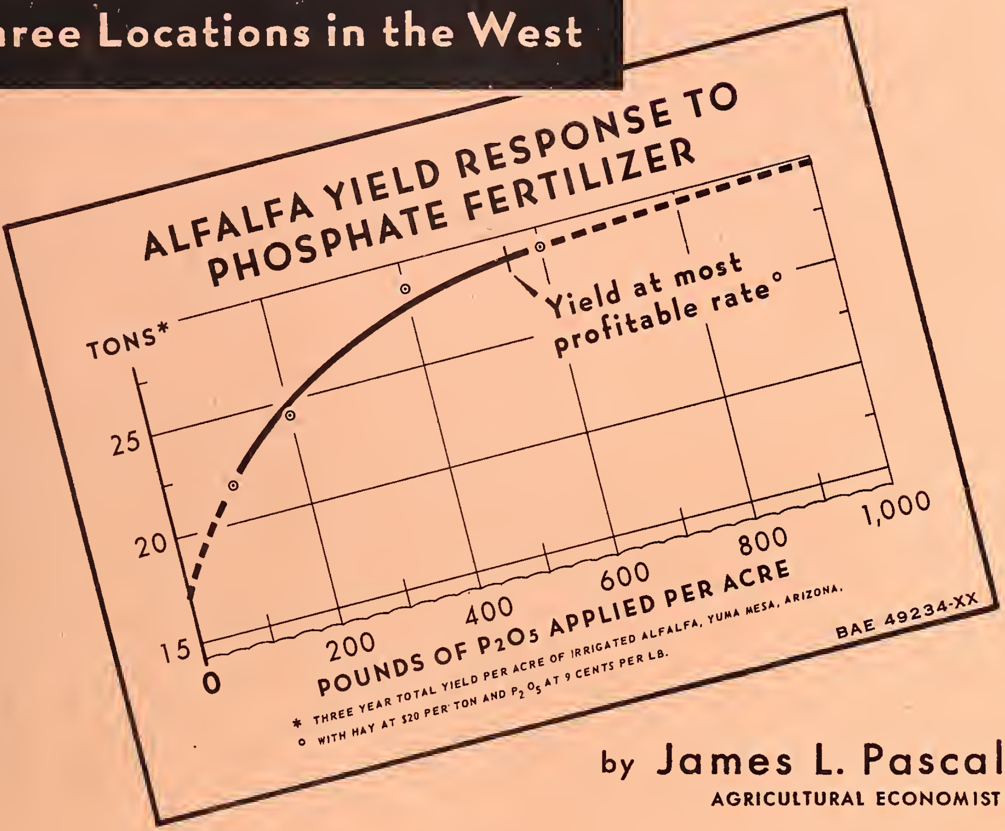

by **James L. Pascal**
AGRICULTURAL ECONOMIST

UNITED STATES DEPARTMENT OF AGRICULTURE
BUREAU OF AGRICULTURAL ECONOMICS

Washington, D. C.
June 1953

PREFACE

This report presents the results of an economic analysis of selected phosphate fertilizer experiments with alfalfa. This work is part of a larger study dealing with economic problems associated with use of fertilizers. Representatives of the Soils Divisions of the Bureau of Plant Industry, Soils, and Agricultural Engineering assisted in making data available, in evaluating the data, and in advising with reference to the many technical details. The author is especially indebted to L. B. Nelson, C. E. Evans, and Omer J. Kelley for assistance toward an understanding of the agronomic aspects essential to appropriate economic interpretation. Assistance in reviewing the manuscript was given by D. B. Ibach, S. W. Mendum, and Warren R. Bailey. Analytical procedures used are those illustrated in "Determining Profitable Use of Fertilizers", U. S. Bur. Agr. Econ. F.M. 105, June, 1953.

SUMMARY

This report presents an economic interpretation of alfalfa yield response to different rates of available P_2O_5 in five experiments on irrigated lands in the West. The fertilizer was applied at the beginning of each experiment and no subsequent applications were made. The analysis was conducted in terms of 3-year total yields. These experimental data are used to illustrate methods of analysis and determination of most profitable rates of fertilizer application. Ways of preparing results for popular presentation to farmers are demonstrated.

The calculated most profitable rates of fertilizer application are high compared with rates commonly applied by farmers in the irrigated areas in which the experiments analyzed are located. All but one of the experiments were located on soils known to be deficient in available phosphorus. With alfalfa at $20.00 a ton and P_2O_5 at $0.09 a pound, the calculated most profitable rates for one Nebraska experiment was 597 pounds of P_2O_5 per acre. Analysis of an experiment in Utah indicated a most profitable rate of 387 pounds. In an experiment in Arizona, the P_2O_5 was applied in conjunction with three different frequencies of irrigation, in which the total water applied during the 3 years was about the same. The calculated most profitable rates there were 553, 581, and 806 pounds of P_2O_5 per acre, depending on the irrigation treatment. In another Arizona experiment the most profitable rate was found to be 843 pounds per acre. The calculated most profitable rate provides a point of departure to be used, with judgment, in making recommendations for individual situations.

Results indicate that for purposes of economic analysis, rate experiments for alfalfa in irrigated areas should include rates of 600 to 800 pounds of P_2O_5 per acre, in most instances. The range in rates should be adequate to include all important increases in yield. Also, a sufficient number of rates should be used to permit accurate description of the yield curve. No fewer than 4 and preferably as many as 6 rates are suggested, but further research is needed to determine the minimum number for different types of situations. Close cooperation between economists and agronomists is needed in planning experimental work and in developing different phases of the analysis.

This analysis is based on the general hypothesis of decreasing increments. Different equations could be used to reflect this hypothesis. The equation $y = M\ (1-R^x)$ is used in this report. In this equation y = the calculated yield; M = the theoretical maximum yield possible as a result of adding fertilizer under conditions of the experiment; R = the ratio of successive increments in yield (a constant less than 1.0); and x = the independent variable (P_2O_5) which, when added in units of uniform size, results in the function represented by R. R^x for a series of units of fertilizer is determined by raising the power of R according to the number of units. Then $1-R^x$ is obtained and multiplied by M to calculate the yield associated with each unit of application. This equation appears to be satisfactory for the yield data used.

ECONOMIC ANALYSIS OF ALFALFA YIELD RESPONSE TO PHOSPHATE FERTILIZER AT THREE LOCATIONS IN THE WEST

By

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Agricultural Economist

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INTRODUCTION

Farmers need to know the rate of application of fertilizer that will return them the most profit. They want to realize the full benefits that fertilizer will bring but they want also to avoid waste. It is easy for them to learn whether fertilizer will increase their yields. They can test it on their own crops or exchange experience with their neighbors. They can study the results of the many tests made at agricultural experiment stations. But usually they cannot get from these sources of information the most profitable rate of fertilizer to use on their own fields.

Experience has shown that generally, throughout the range in practical application increases in yield become smaller from each successive unit of fertilizer added. This observed relationship is commonly known as "the principle of decreasing increments," (8). 1/ The most profitable rate of application is the rate at which the value of additional yields will no more than cover the cost of the additional fertilizer. Neither smaller nor larger applications would pay as well.

The question of the most profitable rate of fertilizer to use on irrigated fields is becoming increasingly important. Both experimental results and farmers' experiences indicate a good response from fertilizer in many areas where water for irrigation is adequate. These findings are reflected in the increased use of fertilizer in the irrigated West. From 1943 to 1950, for example, consumption of nitrogen and phosphate in western States increased threefold. 2/ As more fertilizer is used it will become a larger and larger item in cost of production of crops and therefore of greater consequence to farmers. Farmers who use fertilizer for the first time and those who have used it for some time will be increasingly concerned with its efficient use.

Procedures based on the principle of decreasing increments are used in this report in calculating the physical response and the economic returns from varying rates of commercial fertilizer for specific experiments. This report indicates a method that can be used by agricultural workers to interpret fertilizer response data, how the cost and returns relationships can be analyzed, and how the results can be presented to farmers. The procedure is illustrated by the use of data that show the response in yield of irrigated alfalfa to applied P_2O_5 in five experiments in three western States. Results from these experiments illustrate the variations in yield curves to be found even with one crop and a single plant nutrient. The results also suggest that the most profitable rate of application may be higher than is generally supposed.

1/ Underlined numbers in parentheses refer to Literature Cited, p. 40.

2/ Includes Washington, Oregon, California, Montana, Idaho, Wyoming, Colorado, New Mexico, Arizona, Utah, Nevada, North Dakota, South Dakota, Nebraska, and Kansas. During this period, consumption of nitrogen in these States increased from 47,395 to 166,984 tons and P_2O_5 from 50,024 to 158,503 tons. This increase for each of these nutrients is much greater than for the United States as a whole. National use of nitrogen (N) was 419,000 tons in 1940 and 955,639 tons in 1950. For P_2O_5 consumption rose from 912,000 tons in 1940 to 1,929,878 in 1950.

METHODS USED IN THE ANALYSIS 3/

Economic interpretation of response to fertilizers involves first the characterization of the response curve for crop yields at the various rates of fertilizer application used in the experiment. Once this is accomplished, the rates and combinations of fertilizer that would be most profitable under stated conditions may be calculated.

Developing the Yield Curve

The Equation

Various approaches may be used in characterizing the response curve. The method employed here is based on the general hypothesis that as fertilizer is added in units of uniform size, yields increase at a constantly decreasing rate (4, 8, 9). 4/ The equation, $y = M(1-R^x)$ is a form of an exponential function in which x, the variable, is an exponent of R, the constant ratio of successive increments in yield. 5/ The value of this ratio, R, is always less than 1.0, and its numerical value is determined by the nature of the response as shown by the reported yields, and the size of the unit of fertilizer used in making the calculations. The constant, M, is the theoretical maximum yield that could be obtained with unlimited fertilizer, other conditions remaining the same. The calculated yield, y, for any rate of fertilizer is determined as a percentage of this theoretical maximum yield.

3/ Certain passages describing methods and procedures were prepared jointly by the author of this publication and of F.M. 105, "Determining Profitable Use of Fertilizers," Bur. Agr. Econ. May 1953. Processed.

4/ Unit, as used here, has no relation to the term as used in fertilizer manufacture. Here it refers to a quantity of plant nutrient which may vary among experiments and which for computational purposes, may be varied within the procedure followed.

5/ This equation and procedures for using it in analyzing fertilizer rate experiments involving one or more variables was developed by W. J. Spillman and published as U. S. Dept. Agr. Technical Bulletin 348, "Use of the Exponential Yield Equation in Fertilizer Experiments" (9). More recent exploratory work has resulted in restatement and modification of these procedures, thereby facilitating the work of economic interpretation. See "Determining Profitable Use of Fertilizers" (2).

Figure 1 is a hypothetical illustration of the principle of decreasing increments as expressed by the equation $y = M (1-R^x)$. As shown in this example, the applied portion of the fertilizer nutrient is divided into six equal units. The calculated increment in yield is 3,000 pounds for the first unit of fertilizer, 2,250 pounds for the second, 1,687.5 pounds for the third, and so on. Each yield increment is 75 percent of the one that precedes it. In other words, $R = 0.75$ when the input of fertilizer is divided into six units.

If the calculations are made in such a way that the total fertilizer added is divided into three equal units, the first increment in yield would be 5,250 pounds, the second 2,953.125 pounds, and the third 1,661.13 ≠ pounds. In this case each increment is 56.25 percent of the one preceding it, and $R = 0.5625$. The sum of the increments is the same as before. Thus, when we divide the total added fertilizer into a smaller number of larger units, the effect is to reduce the value of R, without changing the shape of the curve and yields read from it are the same.

The constant M, or maximum yield, is the sum of two other constants Y_0 and A, in which Y_0 is the yield without applied fertilizer and A is the maximum additional yield that can be obtained from fertilizer. The maximum additional yield (A) may be calculated from Y_0 or from any other point on the curve. Thus, M is the sum of A and Y at the point from which A is calculated. These constants likewise are not affected by a change in number of units into which the total input fertilizer is divided. The constant A may be calculated by dividing the first increment in yield by $1-R$. When the fertilizer input is divided into 6 equal units, as noted above, the first increment in yield was 3,000 pounds, R was 0.75, and $1-R$ was 0.25. Therefore, A equals $3{,}000 \div 0.25 = 12{,}000$ pounds. Also, when the total input was divided into 3 units, the first increment was 5,250 pounds, R was 0.5625, and $1-R$ was 0.4375. A equals 12,000 pounds as before ($5{,}250 \div 0.4375$). Therefore, M is the same in each instance because M is equal to A plus the yield at no input of fertilizer. As the yield at no input is 3,000 pounds, $M = 15{,}000$ pounds.

The fact should be emphasized that, to facilitate computations, a determination is made of the size of unit required to render R a specified value. This is done solely, as is illustrated later, to reduce the number of computations required. It is in no way inconsistent with the fact that R (as initially calculated) may have a different value for each experiment. Adjustment in the size of a unit so that R may be expressed as a constant specified decimal fraction saves a great deal of computation because values may be read directly from a prepared table of $1-R^x$ values. Table 8 is such a table, prepared on the basis of $R = 0.80$.

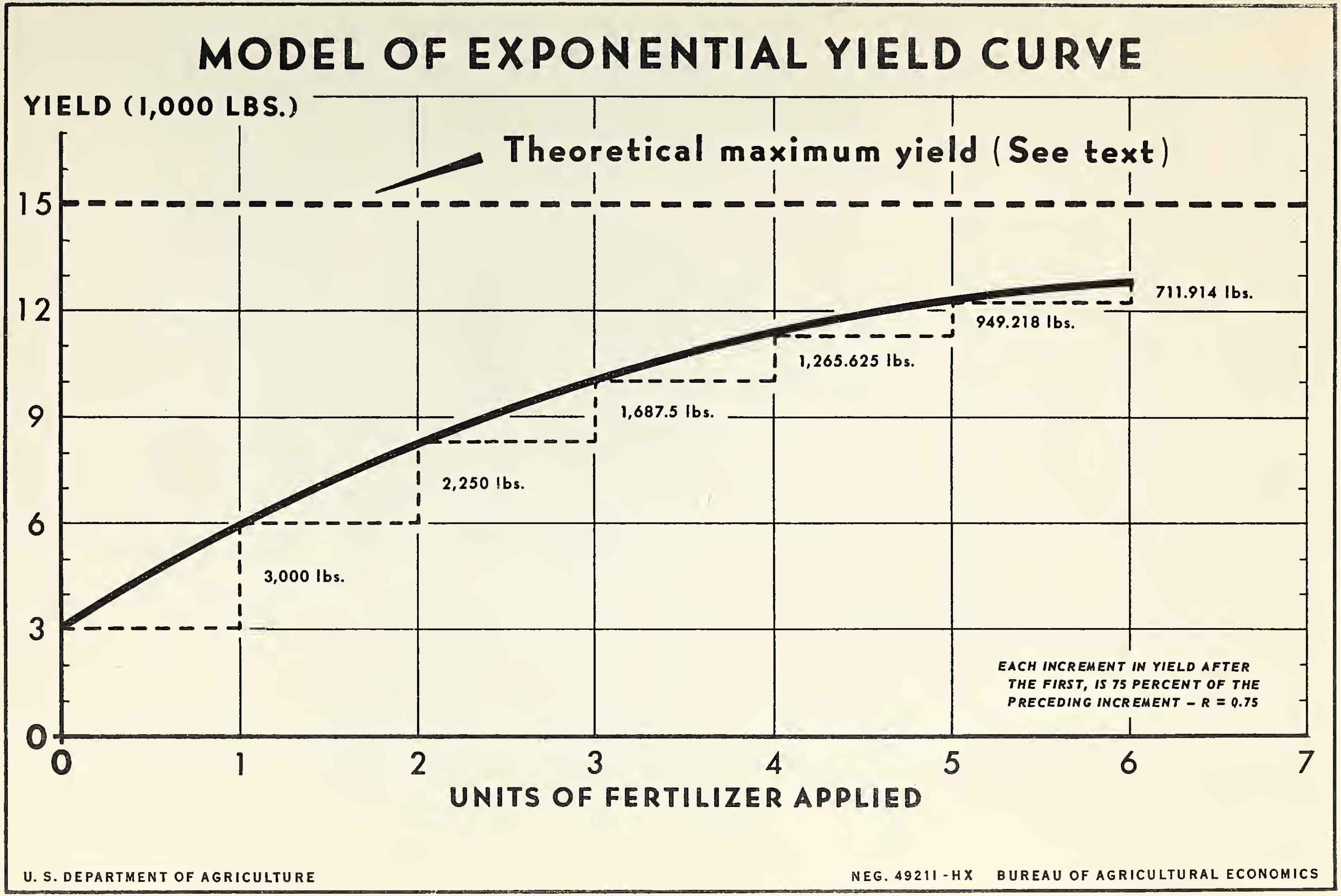
MODEL OF EXPONENTIAL YIELD CURVE
YIELD (1,000 LBS.)
Theoretical maximum yield (See text)
15
12
9
6
3
0
0
1
2
3
4
5
6
7
UNITS OF FERTILIZER APPLIED
3,000 lbs.
2,250 lbs.
1,687.5 lbs.
1,265.625 lbs.
949.218 lbs.
711.914 lbs.
EACH INCREMENT IN YIELD AFTER THE FIRST, IS 75 PERCENT OF THE PRECEDING INCREMENT – R = 0.75
U. S. DEPARTMENT OF AGRICULTURE
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Figure 1

Definitions of Terms and Symbols

The terms and symbols used in developing the yield curve with a single variable are as follows:

1. The yield equation is $y = M\,(1-R^x)$ in which
   y = the calculated yield.

   M = the theoretical maximum attainable yield from adding unlimited units of x, the variable, when other yield-influencing factors remain constant.

   R = the ratio of successive increments in yield--a constant less than 1.0.

   x = the input variable (in this case P_2O_5) which consists of two parts, that contained in the soil and that applied.

   R^x = R raised to the power indicated by the level of x.

   $1-R^x$ = the difference between 1.0 and the x power of R (R^x) at any stated level of the input. It is the function which, multiplied by M, results in the calculated yield.

2. Other constants used in developing the curve and in calculating yields.

   i = the increment in yield associated with the first unit of application; i_2 = the second increment, etc.

   A = the theoretical maximum additional yield that may be obtained from adding the variable, other yield-influencing factors constant.

   Calculation: $A = \dfrac{i}{1-R} = \dfrac{i_2}{[(1-R)-(1-R)^2]}$ etc.

   Y = the reported yield --, Y_o is the reported yield at no application.

   p = calculated quantity of P_2O_5 in the soil measured in the same units as the applied portion.

   Calculation: $(\log M - \log A)/\log 0.8$. This expresses p in terms of units of the size required to render $R = 0.8$. (See definition of u below.) p is one of the components of x, mentioned earlier. When dealing with nitrogen or potash, the comparable quantities of these nutrients are referred to as n and k, respectively.

b = the applied portion of P_2O_5. As used in the equation, it is expressed in terms of units of a size required to render R = 0.8.

Calculation: Pounds of applied P_2O_5 /u (see below). Thus R^x for P_2O_5 becomes R^{p+b}.

u = the number of pounds in a unit of x, or (p+b), required to render R, a specified value, 0.8 as illustrated here.

Calculation: u = log 0.8/log R, times the number of pounds per unit used in determining the value of R.

Thus, any number of pounds applied, b, divided by the determined value of u, expresses b in terms of units. From this point on the term "unit" refers specifically to the quantity of the input variable that would be required to render R = 0.8. The number of units of x, or (p+b) are located in table 15 and the corresponding $1-R^x$ values read from that table. Conversion to a size of unit such that R will equal 0.8 has no significance other than that it simplifies the computations.

Yield Data Used

Experiments dealing with P_2O_5 on irrigated alfalfa are used to illustrate the calculations of the yield curve and of the most profitable rate of fertilizer application. Phosphate fertilizer frequently results in increased yields for several years after application and, for this reason, yield responses should be measured for several years following the initial application of phosphate. Alfalfa is one of the more responsive crops to phosphate fertilizer and as it is a perennial it is well suited to measure the response over a 3-year period. A review (6) in the West through 1949 revealed few field experiments with alfalfa in which the total yield response to initial applications of P_2O_5 was measured for a period of 3 years or longer. However, data from five experiments at three locations on irrigated land in Arizona, Nebraska, and Utah appeared suitable for analysis. The data on yield response in four of these experiments indicated a serious deficiency of available phosphate. A recent survey, however, indicates that phosphate deficiency is not generally serious in most western soils (6). The results presented here, therefore, cannot be considered indicative of any situations except those represented by the experiments.

In all five experiments the fertilizer was applied at the beginning of the test, with no supplemental application made during the 3 years included in this analysis. A brief description of each of the experiments from which data were taken for this study is given in the appendix.

Method of Calculating Constants and Yields

The problem is to develop a smooth curve, any point on which will represent the yield to be expected on the average for the indicated rate of application. No matter what equation is assumed to describe these yields to be expected some method must be employed for estimating the constants in that equation. Frequently the method of least squares is an efficient method of estimation; however, when only a few rates are included, the constants (R, M, A, and others described earlier) may be determined by graphic approximation. When only three rates are given, one may omit the graphing because for this number of rates only one answer is possible. When four or five rates (the maximum number in the experiments analyzed) are used, good results can be obtained by graphic approximation. Data from experiment 2 were used in all steps involved in finding constants of the equation, in calculating yields at any specified rate of application, and in determining the most profitable rate of application. Data used for purposes of illustration comprise total yields for the 3-year period for that portion of the experiment receiving irrigation treatment A.

First, the reported yields for the four rates of P_2O_5 are plotted on graph paper. A smooth curve is drawn freehand to fit these points as closely as possible (fig. 2) The method then involves readings at three points on the freehand curve, one of which is midway between the other two on the X-axis. In this instance, the range used in calculating the value of the constants is that part of the curve between 100 and 600 pounds of applied P_2O_5. Thus the mid-point yield is associated with a rate of 350 pounds and is read as 27.40 tons from the freehand curve. The other two points are the yields associated with rates of 100 and 600 pounds. Readings at the lowest and highest rates need not necessarily be used. The freehand curve does not necessarily pass through any reported yield. Reference to the list of definitions of terms will help to explain the following calculations of constants based on the readings.

1.

(Pounds)	b (Graphic Units)	Y tons	i tons	R (i_2/i)	1-R
100	0	21.84	--	--	--
(350)	1	27.40	5.56	--	--
600	2	29.12	1.72	0.30935	0.69065

2. $A = i/1-R = 5.56/0.69065 = 8.0504$ tons

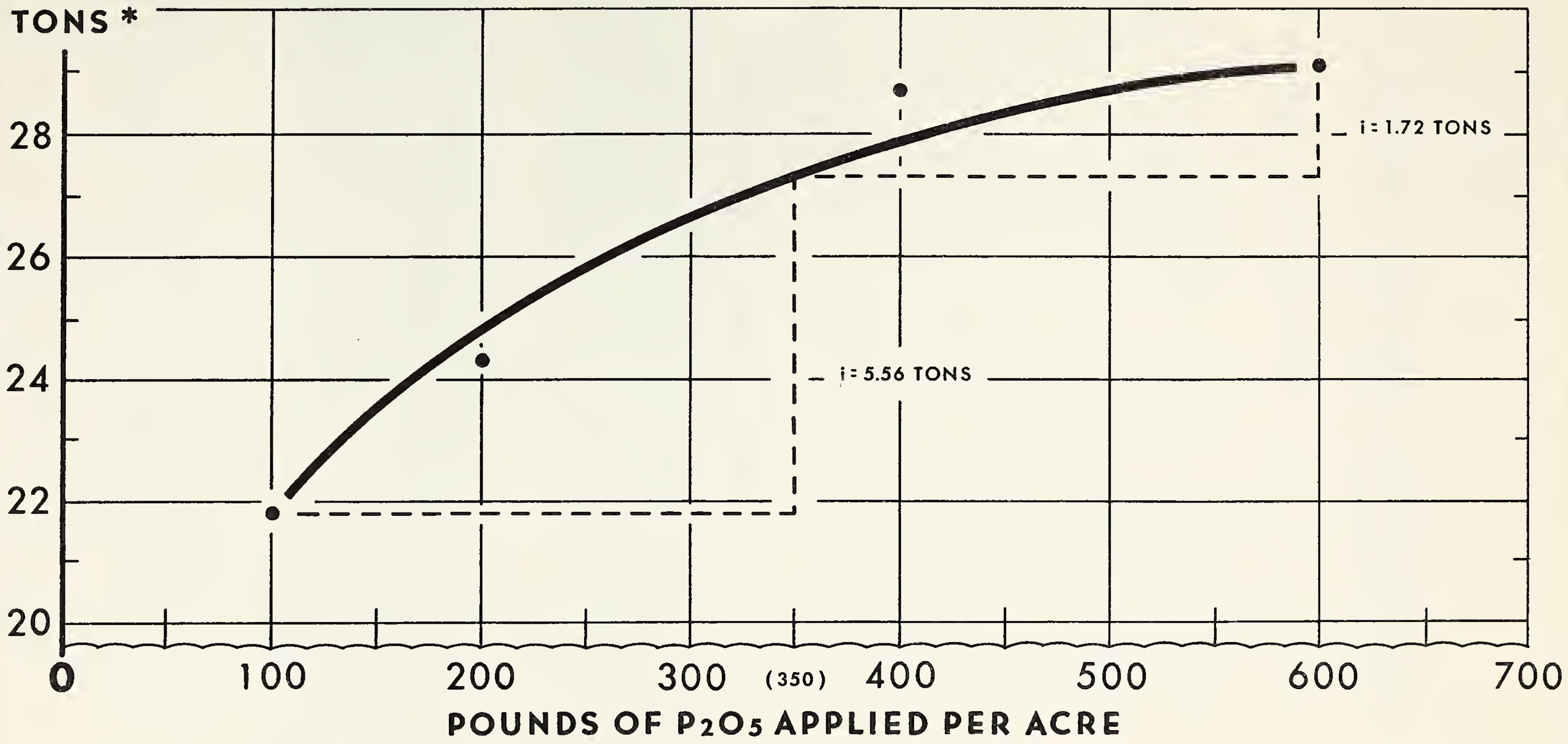
3. $M = A + Y_0 = 29.8904$ tons

4. $\text{Log } R = \log 0.30935 = 9.49045 - 10 = -0.50955$

5. $u = \log 0.8/\log R = -0.09691/-.0.50955 = 0.1902$ 250 lb. units
$= 47.55$ pounds

DETERMINING CONSTANTS OF THE YIELD EQUATION

Yuma Mesa, Arizona



* THREE YEAR TOTAL YIELD PER ACRE OF ALFALFA
BASED ON DATA FROM EXPERIMENT 2, IRRIGATION TREATMENT A

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Figure 2

6. $p + b$ at 0 graphic units (100 lbs. b) $= (\log M - \log A)/\log 0.8$

$= (1.475527 - 0.905817)/-0.09691$

$= 0.569710/-0.09691$

$= 5.8788$ units

Note: When a yield at zero application (reported or read from the freehand curve) is used as one of the points, the result of this calculation is the value of p.

7. Calculation of the 3-year total yields on the P_2O_5 curve:

	x					
b lbs.	b units	p units	$p + b$ units	$1-R^{p+b}$ (From table 8 1/	y tons 2/	Y tons
(0)3/	--	3.7758	3.7758	0.569406	17.02	--
100	2.1030	3.7758	5.8788	.730680	21.84	21.84
200	4.2061	3.7758	7.9819	.831558	24.86	24.31
(350)	7.3607	3.7758	11.1365	.916681	27.40	--
400	8.4122	3.7758	12.1880	.934105	27.92	28.70
600	12.6183	3.7758	16.3941	.974226	29.12	29.12

1/ Values interpolated for fractional units not shown in table 8.

2/ $y = M\ (1-R^{p+b})$

$= 29.8904\ (1-R^{p+b})$

3/ Rates shown in parentheses were not included in the experiment.

Calculating the Most Profitable Rate

The theoretical most profitable rate of P_2O_5 to apply under conditions of this experiment is calculated here, using constants derived in developing the yield curve. It is the rate at which returns above the cost of fertilizer are at a maximum. Either a higher or lower rate results in a smaller return above the cost of fertilizer.

Hay is valued as it stands in the field. From an estimated market price, a stated amount is deducted for harvesting and marketing costs. This procedure does not allow for flexibility in costs of harvesting as the yield increases. Thus, if the deduction per ton for these costs is more than such costs would be at the higher yields, the effect would be to lower the calculated most profitable rate. However, this factor is not usually of sufficient importance to affect the results materially.

Increased yield is the only benefit assigned a monetary value in this presentation but other items, such as quality of crop, nitrogen fixation, response of following crops to residual P_2O_5, and general improvement of soil, may justify evaluation.

Values used in determining the most profitable rate of application are Q and r".

1. $Q = \frac{1}{vM(-\ln R)}$ in which v = the value per unit of the crop less harvesting and marketing costs, and lnR is the natural logarithm of R (0.8 in these illustrations). Thus -lnR is 0.2231435214. This factor is used in the determination of Q. M has been defined earlier.

2. r" = the monetary cost of a unit of b.

   Calculation: Cost of P_2O_5 per pound times u.

The generalized form for calculating the most profitable rate of application of P_2O_5 (b) is as follows:

1. $Q\,r'' = R^{p+b}$ only at the point of maximum returns with respect to fertilizer.

2. $1-R^{p+b}$ is then determined by subtraction and the resulting value is located in table 8.

3. $p+b$ is the x value associated with $1-R^{p+b}$, table 8.

4. Unit value of p, previously determined.

5. Item 3 minus item 4 = most profitable rate in units.

6. Item 5 times u = most profitable rate in pounds.

   Using the method described above, the most profitable rate of application is calculated as shown below. The value of hay standing in the field (v) is taken as $20.00 a ton. The constant, M, has been determined as 29.8904 tons.
   Thus, $Q = 1/(29.8904)(20)(0.22314) = 1/133.39698 = 0.00750$.

The cost of P_2O_5 is taken as $ 0.09 a pound. As u in the preceding calculations is 47.55 pounds, r", the cost of this quantity of P_2O_5 is $ 4.2795. Thus, Qr", or $R^{p+b} = 0.03210$. Hence, $1-R^{p+b}$ is 0.96790. Referring to table 8, the corresponding x value is 15.41 units. As p has been determined as 3.78 units, b is 11.63 units of 47.55 pounds each, or 533 pounds. This is the calculated most profitable rate applied at the beginning of the experiment indicated by the total response over a 3-year period.

RESULTS AND DISCUSSION

A method of establishing a yield curve and for calculating the most profitable rate of fertilizer application has been illustrated in the preceding pages. Results from this method applied to data from five experiments on alfalfa fertilized with P_2O_5 are now presented and discussed. Each experiment is briefly described in the appendix. These results necessarily apply only to the conditions of the experiments, but may serve as a guide in similar situations. The problem of translating these results into recommendations will be discussed later.

Alfalfa Hay Yield Curves

Seven yield curves were prepared, four for Arizona, two for Nebraska, and one for Utah. The constants necessary to calculate yields for any given rate of P_2O_5 application for each experiment are shown in table 1. The calculated yields for the rates actually applied and for some additional rates are shown in table 2. These calculated yields in turn were used to construct the curves for experiment 2 shown in figure 3 and for experiments 1, 3, 4, and 5 shown in figure 4. It may be noted that the reported yields all lie fairly close to the curve in each case.

The relationship of irrigation practice in combination with different rates of applied P_2O_5 is shown in the yield curves for irrigation treatments A, B, and C (fig. 3). Approximately the same amount of water was applied over the 3 years in each instance. But in treatment A the water was applied in relatively large and infrequent irrigations; in treatment B in moderately large irrigations at medium intervals and in treatment C in small but frequent intervals. Higher yields were associated with the more frequent small irrigations, especially at the higher rates of fertilization. When no fertilizer was applied, yields were not reported. However, the yields calculated when no P_2O_5 was applied were about the same for all irrigation treatments.

These data are in agreement with the general experience that adequate moisture is essential to most efficient use of fertilizers. Thus, both irrigation practice and rates of application of fertilizer must be evaluated in determining the most profitable combination of these two factors of growth. The costs of the water and of its application are not considered in this report, which is limited to economic interpretation of use of fertilizer as a single variable. But it should be noted that at rates of 400 and 600 pounds of P_2O_5 applied per acre, 3-year total yields were about 8 tons more per acre for irrigation treatment C than for treatment A.

The differences in the yield curves for irrigation treatments A, B, and C reflect the effect of different yield influencing factors, which presumably in this instance are primarily differences in fertilizer and water treatments. Because of this fact different constants are found for the yield equation derived from

Table 1.- Calculations of most profitable rates of P_2O_5 per acre and returns above cost of fertilizer based on 3-year total yields of irrigated alfalfa for 5 experiments studied 1/

Items of calculation 2/	Unit	Arizona experiments				Nebraska experiments		Utah experiment
		1 (YM 1)	2 (YM 76)			3	4	5
			Irrigation treatments			(Minatare)	(Mitchell)	(Millville)
			A	B	C			
1. M	Ton	26.0290	29.8904	35.9210	38.7230	22.5080	18.2183	16.1350
2. Q	-	.00861	.00750	.00624	.00579	.00996	.01230	.01389
3. u	Pound	62.662	47.550	79.692	40.822	48.612	5.994	32.269
4. r" (u times .09)	Dollar	5.64	4.28	7.17	3.67	4.38	0.54	2.90
5. Qr" (R^{p+b})	-	.04856	.03210	.04474	.02125	.04362	.00664	.04028
6. $1-R^{p+b}$	-	.95144	.96790	.95526	.97875	.95638	.99336	.95972
7. p + b	Unit	13.56	15.41	13.92	17.26	14.04	22.47	14.39
8. p	do.	.11	3.78	3.81	3.02	1.75	7.95	2.67
9. b	do.	13.45	11.63	10.11	14.24	12.29	14.52	11.72
10. b times u 3/	Pound	843	553	806	581	597	87	378
11. Yield (M times item 6)	Ton	24.7650	28.9309	34.3139	37.9001	21.5262	18.0973	15.4851
12. v	Dollar	20.00	20.00	20.00	20.00	20.00	20.00	20.00
13. Gross return	do.	495.30	578.62	686.28	758.00	430.52	361.95	209.70
14. Cost of fertilizer (r" x item 9)	do.	75.86	49.78	72.49	52.26	53.83	7.84	33.99
15. Return above fertilizer cost 4/	do.	419.44	528.84	613.79	705.74	376.69	354.11	275.71

1/ With hay priced at $20.00 a ton and P_2O_5 at $0.09 a pound.

2/ Definition of symbols and method of calculating their values were shown earlier.

3/ Most profitable rates.

4/ Return available to pay all costs except fertilizer.

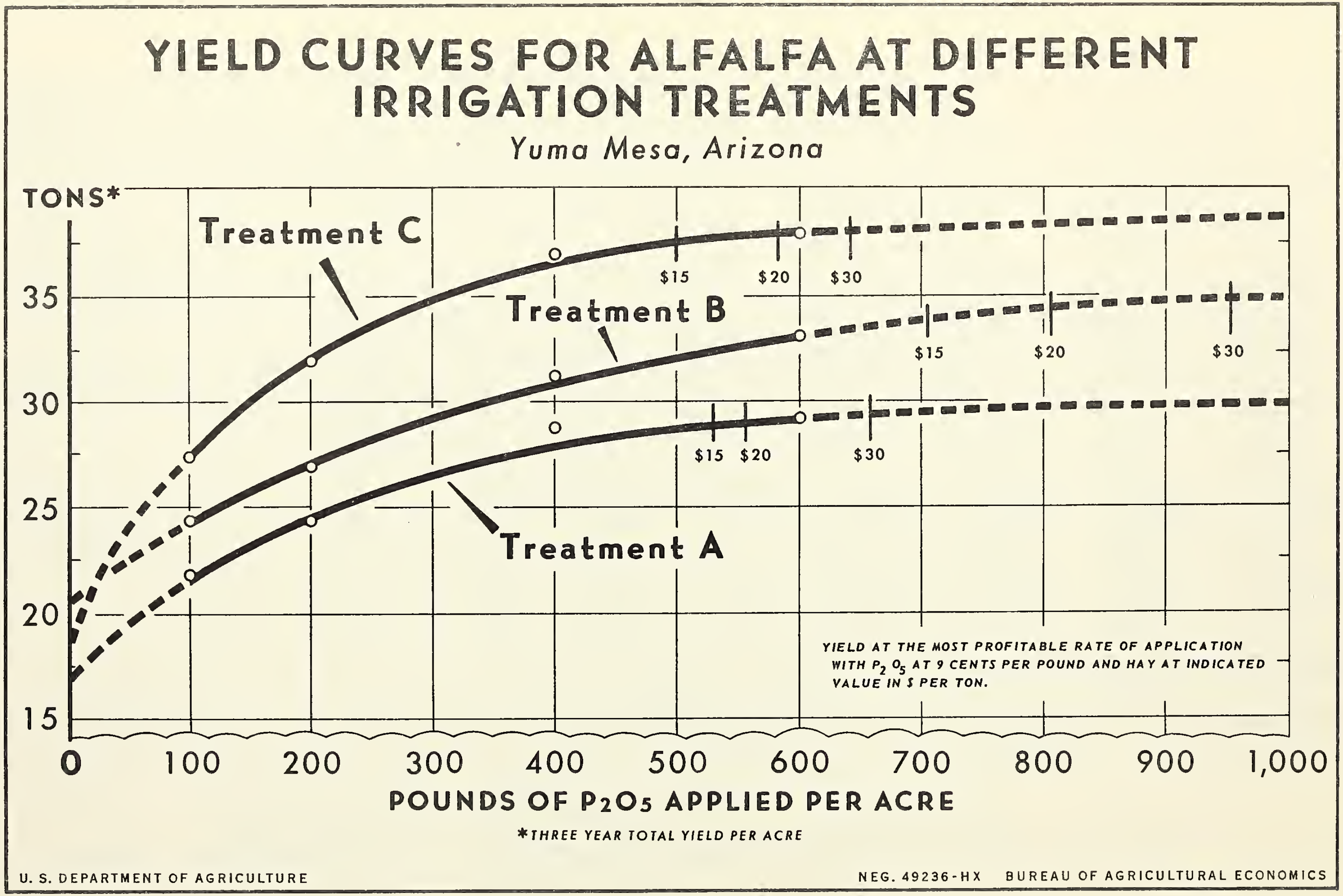
YIELD CURVES FOR ALFALFA AT DIFFERENT IRRIGATION TREATMENTS
Yuma Mesa, Arizona
TONS*
35
30
25
20
15
Treatment C
Treatment B
Treatment A
$15
$20
$30
$15
$20
$30
$15
$20
$30
YIELD AT THE MOST PROFITABLE RATE OF APPLICATION WITH P2 O5 AT 9 CENTS PER POUND AND HAY AT INDICATED VALUE IN $ PER TON.
0
100
200
300
400
500
600
700
800
900
1,000
POUNDS OF P2O5 APPLIED PER ACRE
*THREE YEAR TOTAL YIELD PER ACRE
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Figure 3

Table 2.- Calculated 3-year total yields per acre of alfalfa at different rates of P_2O_5 applied only in the first year [1]

P_2O_5 applied per acre	Arizona experiments				Nebraska experiments		Utah experiment
	1 (YM-1)	2 (YM-76) Irrigation treatment			3 (Minatare)	4 (Mitchell)	5 (Millville)
		A	B	C			
Pounds	Tons	Tons	Tons	Tons	Tons	Tons	Tons
0.0	(0.60)[2]	(17.02)	(20.57)	(18.99)	7.29	15.13	7.24
31.5					9.34	17.26	
45.0					10.13	17.64	
50.0							9.84
67.5					11.35	18.03	
90.0					12.44	18.11	
100.0	8.22	21.84	24.32	27.30	(12.89)	(18.14)	11.68
200.0	13.56	24.86	27.15	32.11	(16.43)		(13.90)
400.0	19.91	27.92	30.91	36.51	(20.08)		(15.58)
600.0	(23.03)	29.12	33.06	37.98	(21.54)		(15.99)
800.0	(24.56)	(29.61)	(34.29)	(38.47)	(22.12)		(16.10)
900.0	(25.00)	(29.70)	(34.68)	(38.58)	(22.26)		
1000.0	(25.31)	(29.77)	(34.99)	(38.64)	(22.35)		

[1] Yields in parentheses are extrapolations.

[2] The calculated yield at zero-rate of P_2O_5 is much lower in this experiment than in experiment 2, although both were conducted on virgin Superstition fine sand. No information is available to explain the discrepancy.

reported yields for the same rates of application of P_2O_5 but for different irrigation treatments. For example, the value of R is a mathematical expression of the character of the curve. At any specified size of unit, the higher the numerical value of R the more gradual but more sustained is the slope of the curve. Conversely, the lower the value of R, the more abrupt is the rise of the curve and the more rapidly it flattens as it moves in the direction of M. This is brought out in figure 3. When R is found in terms of a unit of 50 pounds, the lowest R value for the 3 curves is 0.76. This is for irrigation treatment C, for which the curve rises abruptly from the start. This means that on this sandy soil smaller but more frequent irrigations resulted in obtaining a larger proportion of the total response to each successively higher rate of application of P_2O_5, than did the treatments representing the less frequent irrigations. The other two curves, particularly the one for irrigation treatment B, rise less rapidly but the rise is sustained longer. The R value for irrigation treatment B is 0.87, when found in terms of 50-pound units. For irrigation treatment C, the value of R is 0.79. These numerical values of R (size of unit constant) reflect the nature of the curve, which in turn is a reflection of all the conditions of the experiment.

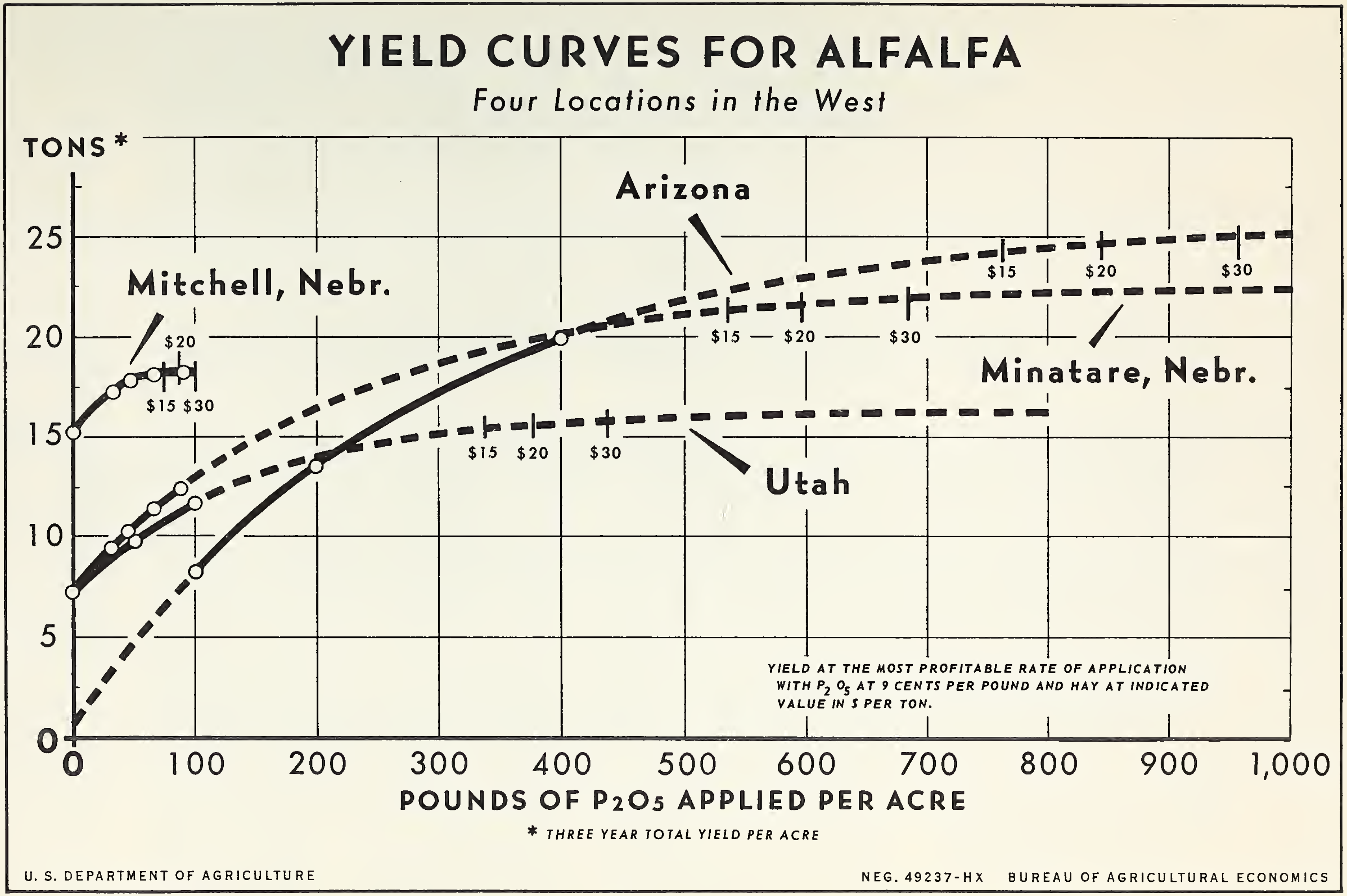
The greater parts of the yield curves for experiments 3 and 5 (fig. 4) were projected beyond the range of recorded yields because of the relatively low maximum rates of fertilizer applied in the experiments. The validity of these projected curves could be determined more definitely by additional trials that would include higher rates of fertilizer.

The Most Profitable rate of P_2O_5 Application

The discussion now turns to the location of the point on these yield curves that is associated with the most profitable rate of application. It may be recalled that this is also the point at which total returns from the crop above the cost of fertilizer are maximized. More or less fertilizer (even a small quantity) would reduce the net return. We can illustrate these facts, again using data from experiment 2, irrigation treatment A (table 1). The most profitable rate, (with alfalfa at $20.00 a ton and P_2O_5 at 9 cents a pound) was found to be 553 pounds of P_2O_5 per acre, and the corresponding yield was 28.9309 tons of hay over a 3-year period. Computations at this 553-pound rate and at 548 and 558 pounds, follow:

P_2O_5 applied	Yield	Value of total yield	Total cost of fertilizer	Returns above cost of fertilizer	Additional yield		Additional fertilizer	
					Quantity	Value	Quantity	Cost
Lbs.	Tons	Dols.	Dols.	Dols.	Tons	Dols.	Lbs.	Dols.
548	28.9067	578.13	49.32	528.81				
553	28.9309	578.61	49.77	528.84	0.0242	0.48	5	0.45
558	28.9518	579.03	50.22	528.81	.0209	.42	5	.45

Note that return above cost of fertilizer is highest, $528.84, when 553 pounds of P_2O_5 are applied. The return is slightly lower, $528.81, when 548 pounds are applied, and it is also $528.81 when 558 pounds are applied. The most profitable rate is also where the value of the last increment in yield equals the cost of the added fertilizer. At the 553-pound rate the last 5 pounds of P_2O_5 added, costing $0.45, results in an increment of 0.0242 tons of hay worth $0.48. At the 558-pound rate, the last 5 pounds of P_2O_5 resulted in an increment of 0.0209 tons, worth $0.42. At this rate, the value of the incremental



YIELD CURVES FOR ALFALFA

Four Locations in the West

YIELD AT THE MOST PROFITABLE RATE OF APPLICATION WITH P_2O_5 AT 9 CENTS PER POUND AND HAY AT INDICATED VALUE IN $ PER TON.

* THREE YEAR TOTAL YIELD PER ACRE

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Figure 4

yield does not cover the added cost of fertilizer. The fact that the most profitable rate of application of fertilizer is also the one at which the additional cost is just covered by the additional value of production, is useful in ascertaining the most profitable rate for various price relationships.

For practical use, a table of yield increments may be prepared showing small units of P_2O_5, such as 20 pounds. (table 3). From this table the most profitable rate for conditions represented by the experiment can be located to the nearest 20-pound unit. This most profitable rate is found by locating in the table that yield increment the value of which covers the cost of 20-pounds of P_2O_5, then reading the associated rate of fertilizer application. For instance, with P_2O_5 at $0.09 a pound, a 20-pound unit costs $1.80, and with hay at $20 a ton an increment of 0.09 tons is required to cover that cost. Continuing with experiment 2-A, the increment in table 3 nearest 0.09 is 0.0915 tons and the associated rate of P_2O_5 application is 560 pounds.

The most profitable rate of P_2O_5 application for other prices of hay and P_2O_5 can also be ascertained from this table. Suppose P_2O_5 remains at $0.09 a pound but hay is $30.00 a ton. The cost of a 20-pound unit is again $1.80, but now, only 0.06 ton of hay is required to cover that cost. Reading from the table, we find the nearest yield increment is 0.0627, and it is associated with an application of 640 pounds of P_2O_5. With hay at $15.00 a ton it takes 0.12 tons of hay to cover the cost of a 20-pound unit of P_2O_5. The nearest yield increment is 0.1213, which is associated with a rate of 500 pounds of P_2O_5. This is the most profitable rate of application. Other prices of hay and P_2O_5 can be readily substituted.

For various reasons, some farmers may decide to apply somewhat fewer units of fertilizer than the calculated most profitable rate. The net returns on the last units of P_2O_5 are small. Adverse growing conditions could nullify part of the potential response. A farmer having inadequate capital might prefer to use part of his funds to improve some other yield-limiting factor such as an inadequate irrigation system. These considerations are pertinent in view of the limitations surrounding the estimates.

For farms on which production conditions and the yield curve appear to be the same as those on an experiment such as 2-A, the most profitable rates may serve as a direct guide. Other farms with the same characteristics of yield but with a lower or higher level of yield will require adjustments in the rate scale. For example, on a farm having the same characteristics, but with yield at no application the same as the experimental yield at 200 pounds, that is 24.86 tons, the scale would be adjusted as follows:

Fertilizer	
Farm units	Experiment units
0	200
xxx	xxx
320	520
340	540
360	560

Table 3.- Calculated yield increments of alfalfa per acre for a 3-year period, associated with each additional 20-pound unit of P_2O_5 in one application at the beginning of the experiment 1/

P_2O_5 applied per acre		Experiments						
		1	2			3	4	5
			Treatments					
			A	B	C			
Pounds	Units	Tons	Tons	Tons	Tons	Tons	Tons	Tons
0		-	-	-	-	-	-	-
20	1	1.7480	1.1530	0.8362	2.0435	1.3348	1.6220	1.1491
40	2	1.6274	1.0497	.7906	1.8392	1.2178	.7704	1.0007
60	3	1.5160	.9550	.7461	1.6415	1.1112	.3657	.9322
80	4	1.4118	.8710	.7094	1.4719	1.0134	.1738	.6980
100	5	1.3147	.7918	.6681	1.3204	.9244	.0827	.6610
120	6	1.223	.7219	.6304	1.1950	.8437	.0390	.5754
140	7	1.1402	.6561	.5974	1.0482	.7695	.0184	.5013
160	8	1.0618	.5981	.5640	.507	.7016	.0087	.4366
180	9	.9888	.5440	.5356	.851	.6408	.0041	.3797
200	10	.9233	.4950	.5050	.7640	.5843		.3311
220	11	.8547	.4510	.4770	.6854	.5330		.2882
240	12	.7986	.4107	.4516	.6130	.4862		.2509
260	13	.7456	.3739	.4271	.5510	.4438		.2184
280	14	.6903	.3408	.4030	.4933	.4050		.1906
300	15	.6452	.3096	.3826	.4423	.3686		.1657
320	16	.6005	.2822	.3599	.3969	.3372		.1544
340	17	.5591	.2568	.3419	.3551	.3070		.1255
360	18	.5209	.2337	.3219	.3186	.2805		.1097
380	19	.4849	.2128	.3057	.2858	.2554		.0952
400	20	.4519	.1937	.2888	.2560	.2337		.0830
420	21	.4201	.1767	.2723	.2296	.212		.0723
440	22	.3922	.1611	.2579	.2056	.1943		.0630
460	23	.3655	.1458	.2443	.1844	.1771		.0549
480	24	.3389	.1331	.2302	.1653	.1619		.0476
500	25	.3165	.1213	.2180	.1483	.1472		.0416
520	26	.2944	.1100	.2062	.1328	.1346		.0362
540	27	.2751	.1007	.1951	.1170	.1228		.0316
560	28	.2546	.0915	.1843	.1068	.1117		.0274
580	29	.2381	.0831	.1745	.0980	.1022		.0239
600	30	.2215	.0759	.1646	.0856	.0929		.0208
620	31	.2070	.0694	.1558	.0771	.0851		.0181
640	32	.1918	.0627	.1470	.0689	.0774		.0159
660	33	.1786	.0568	.1397	.0619	.0709		.0137
680	34	.1668	.0520	.1315	.0554	.0646		.0121
700	35	.1551	.0479	.1243	.0496	.058		.0104
720	36	.1448	.0433	.1181	.0445	.0536		.0091
740	37	.1345	.0401	.1110	.0399	.0490		.0080
760	38	.1252	.0349	.1053	.0360	.0448		.0067
780	39	.1169	.0323	.0998	.0325	.0407		.0062
800	40	.1085	.0299	.0942	.0264	.0372		.0051
820	41	.1004		.0889				
840	42	.0929		.0839				
860	43	.0860		.0792				

1/ In using this table to find the most profitable rate, divide the cost of 20 pounds of P_2O_5 by the price per ton of hay standing in the field. The result is the fraction of a ton of hay equal in value to 20 pounds of P_2O_5. Locate this result in the appropriate column and from the left-hand column read the rate of application with which it is associated. This is approximately

From table 3 the rate on the farm scale associated with 0.09 would apply. 6/ That rate would be about 360 pounds compared with 560 for the experiment. Or the "farm scale" could be adjusted to figure 5.

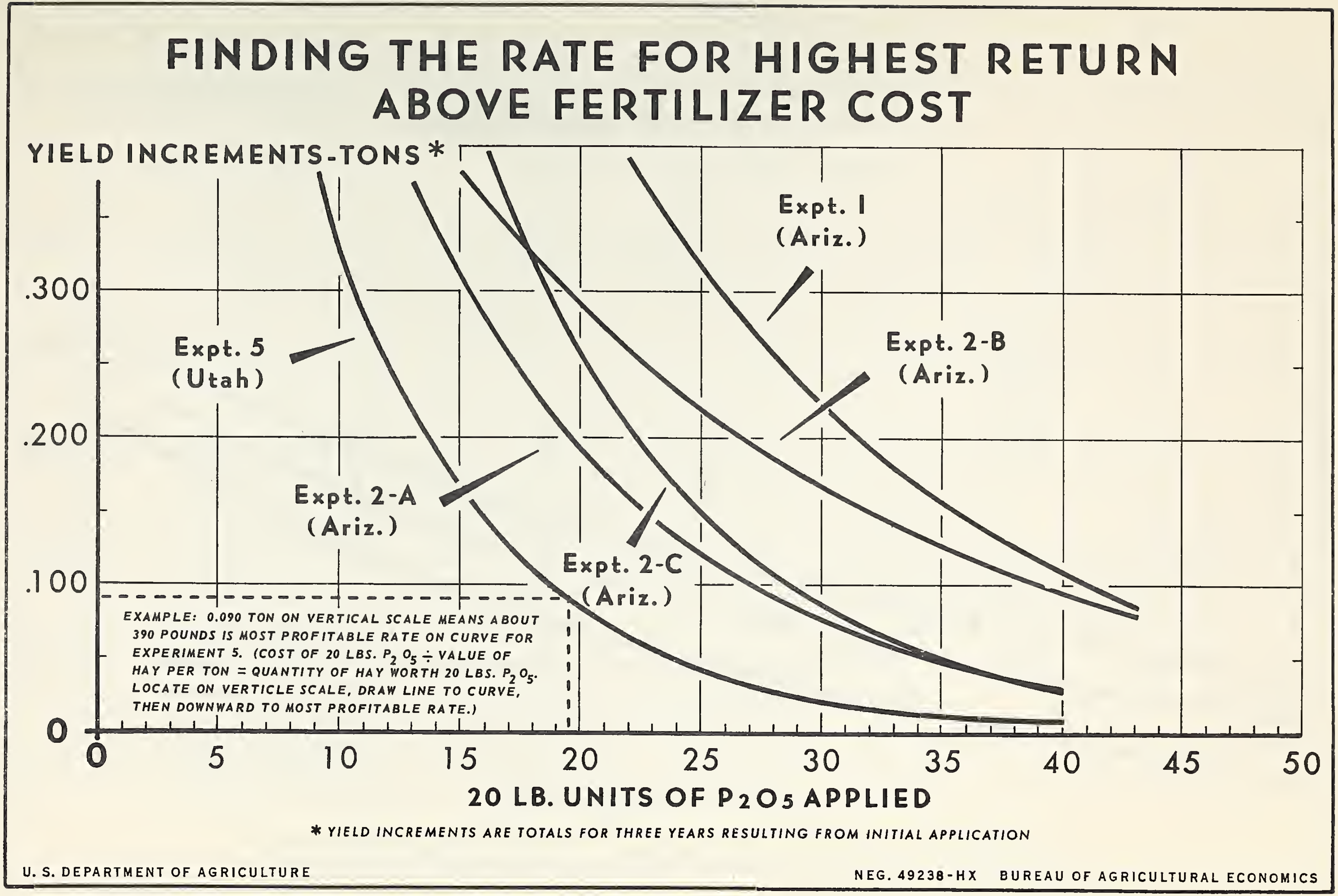
The approximate most profitable rate at given price relationships may also be determined by the use of yield increment curves, as shown in figure 5. In this figure the yield increments (smaller than 0.4401) taken from table 3, are plotted against P_2O_5 applications on the base scale and against a scale of increments on the vertical scale. The most profitable rate of application is found as before. First, the size of yield increment necessary to cover the cost of a 20-pound unit of P_2O_5 is calculated. Then the increment nearest this size is located on the increment (vertical) scale. Reading across, the corresponding point is found on the curve and the rate of application is read on the base scale. This again is approximately the most profitable rate.

For use in an educational meeting, the most profitable rate of fertilization, for a given situation, may be presented effectively in a somewhat simpler way as shown in figure 6. In this chart, most profitable yield curves are drawn for three alternative prices of P_2O_5, and for prices of alfalfa hay ranging from $10.00 to $50.00 a ton.

A farmer who plans to make a planting of alfalfa will know approximately the going price of P_2O_5, but the price of hay in the next 3 years is less certain. Moreover, some farmers regularly produce hay of higher or lower quality than the average. Prospective or probable prices of hay are discussed and each farmer can establish his own assumed price. From the chart, the most profitable rate of application of fertilizer can be determined for any of the assumed prices of hay, whether P_2O_5 is figured at the going price or at an alternative price above or below the going price. From the assumed price of alfalfa on the base scale of the chart, a point is located on the curve; from this point the most profitable rate is read on the vertical scale.

The calculated most profitable rate is not intended as a final answer for either a specific experimental site or a general area. It is, however, the result of a specific definable procedure which may be altered if necessary, as experiments and experience suggest: as such it serves as a sound basis for deciding how much fertilizer to apply.

6/ 0.09 = tons of hay at $20.00 a ton required to pay for 20 pounds of P_2O_5 at $0.09 a pound: $\frac{1.80}{20.00} = 0.09$.



FINDING THE RATE FOR HIGHEST RETURN ABOVE FERTILIZER COST

EXAMPLE: 0.090 TON ON VERTICAL SCALE MEANS ABOUT 390 POUNDS IS MOST PROFITABLE RATE ON CURVE FOR EXPERIMENT 5. (COST OF 20 LBS. P_2O_5 ÷ VALUE OF HAY PER TON = QUANTITY OF HAY WORTH 20 LBS. P_2O_5. LOCATE ON VERTICLE SCALE, DRAW LINE TO CURVE, THEN DOWNWARD TO MOST PROFITABLE RATE.)

* YIELD INCREMENTS ARE TOTALS FOR THREE YEARS RESULTING FROM INITIAL APPLICATION

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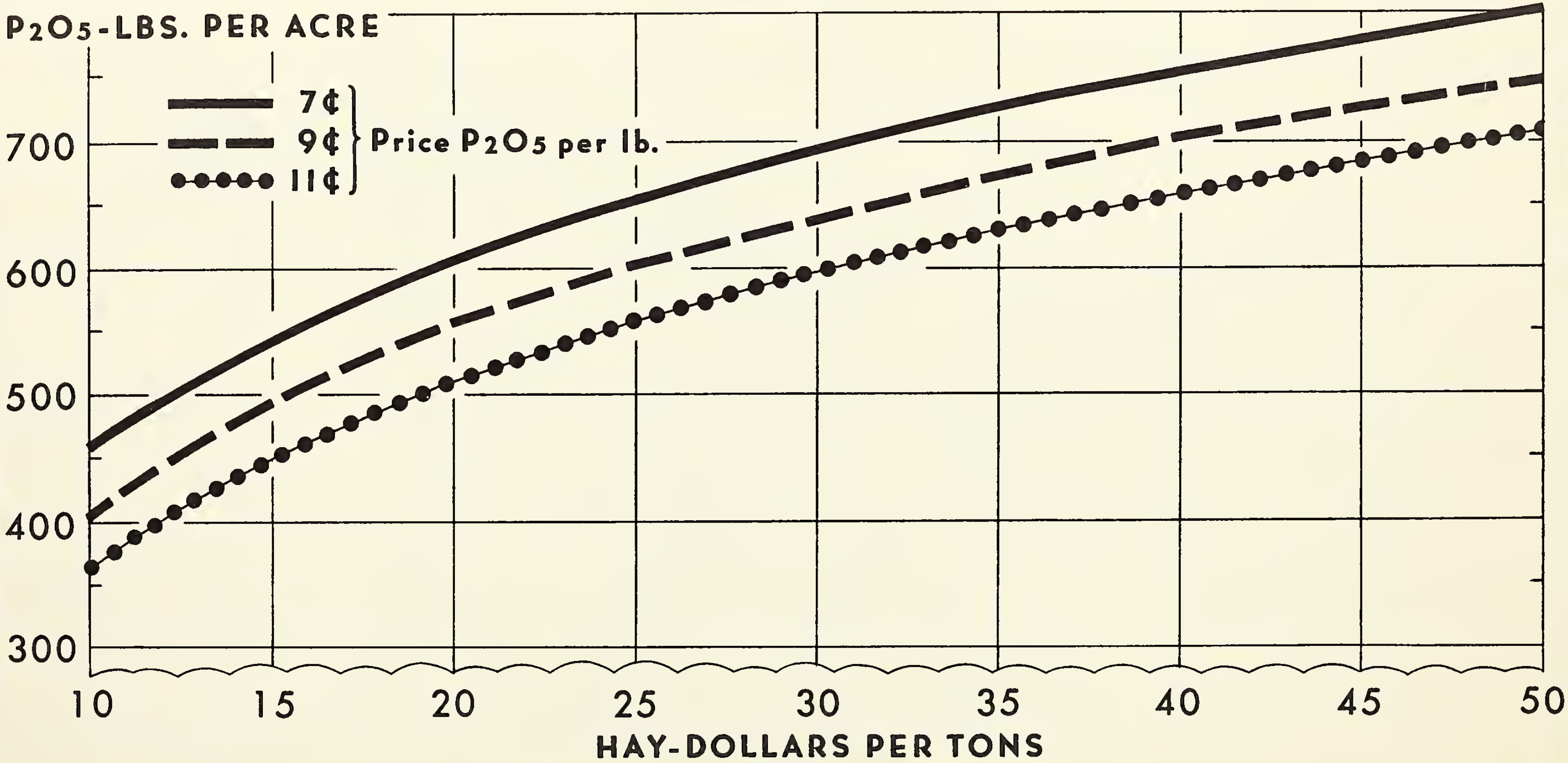
Figure 5

MOST PROFITABLE RATE OF P_2O_5 FOR ALFALFA AT DIFFERENT PRICES AND COSTS

Yuma Mesa, Arizona



BASED ON DATA FROM EXPERIMENT 2, IRRIGATION TREATMENT A

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Figure 6

It is of interest to compare the most profitable rates of application for the 5 experiments, when alfalfa hay is $20.00 a ton and P_2O_5 is $0.09 a pound. These rates are as follows:

Experiment		Most profitable rate of P_2O_5
		Pounds
No. 4 (Nebraska)		87
No. 5 (Utah)		387
No. 1 (Arizona)		843
No. 2 (Arizona)	Treatment A	553
	Treatment C	581
	Treatment B	806
No. 3 (Nebraska)		597

These rates are high compared with those commonly applied by farmers in the respective irrigated areas, but the experiments were located on soils known to be deficient in available phosphorus.

The most profitable rates are also greater than the highest rates actually applied in all of the experiments, except treatments A and C of experiment 2. (See figs. 3 and 4). In treatments A and C the most profitable rate (with hay at $20.00 and P_2O_5 at $0.09) is almost as great as the highest rate actually applied. It appears that even higher rates of P_2O_5 should have been applied in all of the experiments.

Only the averages of replicated plot yields were readily available for purposes of this report. It is recognized that testing of individual plot yields for variance would have contributed to a better appraisal of the calculated yields and the calculated most profitable rates. Analysis of variance and determination of standard errors of reported yields would help answer the question of how closely to follow the calculated most profitable rates in commercial operations.

Yield benefits from applied P_2O_5 may extend over a period of several years as shown by experiments used here. (Appendix tables 4, 5, 6, and 7.) Yield response to residual fertilizer also has been noted for other crops and nutrients. When such residual effects are of practical significance they too should be evaluated in calculating the most profitable rate of application. Heavy yield response following the year of application suggests later application at various other rates. Such information may be used to appraise the economic aspects of single vs. multiple applications.

Other benefits in addition to yield response may be of economic importance. For example, quality is a significant factor with some crops. Increase in protein content frequently is important in livestock feeding. Fixation of nitrogen by legumes also may be of economic significance. When these benefits appear to be noteworthy they should be investigated also as a part of rate studies, because they may influence significantly the selection of the most profitable rate of fertilizer application.

As the purpose of a fertilizer rate experiment is to supply information for recommendations as to rates, description of the test conditions of the experiment needs to be complete. The kind of soil, fertilizer history, and crop history of the plots are essential information. Description of cultural practices, especially on stands, irrigation practice, disease and insect control, and other pertinent items help in deciding as to the feasibility of specific fertilizer practice under farm conditions. It is necessary to report the kind of fertilizer and the time and manner of application.

The final objective of most fertilizer rate experiments is to formulate recommendations to farmers; therefore, both the agronomic and the economic phases need attention. Close cooperation is desirable between the soil scientist who conducts the experiment and the economist who is to make the economic analysis of the data.

APPENDIX

Agronomic Data

A brief description of each experiment from which data were taken for economic analysis follows:

The Arizona Experiments

Data were used from two alfalfa experiments on virgin Superstition fine sand at Yuma Mesa, Ariz. This soil is low in available phosphate and its water-holding capacity is low also.

Experiment YM-1 had been designed to measure the residual effects of different kinds of phosphate fertilizers on alfalfa yields. The portion of this experiment that is analyzed here received double superphosphate, broadcast at rates of 100, 200, and 400 pounds of P_2O_5 per acre. These applications, replicated four times, were made at seeding time in the fall of 1945. Earlier in that year all plots had been treated with 100 pounds of P_2O_5 per acre and seeded to sudan grass to protect the later seeding of alfalfa. Yields of alfalfa hay were reported for 1946, 1947, and 1948.

Table 4.- Reported yields of alfalfa at 3 rates of P_2O_5 applied as double-superphosphate in 1945 - Experiment YM-1, Yuma Mesa, Ariz. 1/ 2/

P_2O_5 applied per acre	Reported yields per acre			
	1946	1947	1948	Total
Pounds	Tons	Tons	Tons	Tons
100	1.691	3.362	3.163	8.216
200	2.993	5.571	5.185	13.749
400	5.142	8.231	6.533	19.906

1/ This is referred to in the text as experiment 1.
2/ From "Alfalfa for Yuma Mesa", U. S. Dept. Agr. Cir. 879, August 1951 (1).

Experiment YM-76, referred to in the text as experiment 2, and started in 1948, measured the response to different initial rates of P_2O_5, and various irrigation treatments (10). Applications of P_2O_5 were made in the fall of 1948 and were drilled in bands 4 inches deep between rows of Sudan grass. The alfalfa was then seeded directly over the banded phosphate application. Three irrigation treatments, each representing a different frequency of irrigation, but with little difference in total quantity of water applied, were used.

Table 5.- Reported yields of alfalfa at 4 rates of P_2O_5 applied at seeding time in the fall of 1948 - Experiment YM-76, Yuma Mesa, Ariz. 1/

Frequency of irrigation	P_2O_5 applied per acre	Reported yields per acre			
		1949	1950	1951	Total
	Pounds	Tons	Tons	Tons	Tons
Low (A)	100	9.64	8.26	3.95	21.84
	200	9.40	9.79	5.12	24.31
	400	10.93	10.92	6.85	28.70
	600	11.46	10.84	6.82	29.12
Medium (B)	100	10.66	8.80	4.86	24.32
	200	9.54	10.69	6.70	26.93
	400	11.81	11.53	7.79	31.13
	600	11.80	12.23	9.02	33.06
High (C)	100	11.01	10.85	6.44	27.30
	200	11.02	13.34	7.63	31.99
	400	11.88	14.31	10.44	36.63
	600	10.94	15.03	12.01	37.98

1/ Unpublished data furnished by C. O. Stanberry, Division of Soil Management - Irrigated and Dryland Regions, Bureau of Plant Industry, Soils, and Agricultural Engineering. USDA (10).

The Nebraska Experiments

Data from two experiments were analyzed (3), one on Mitchell silt loam and one on Minatare silt loam in the North Platte Valley of western Nebraska (table 6).

Table 6.- Reported yields of alfalfa at no application and at 4 rates of P_2O_5 applied on two soils, North Platte Valley, western Nebraska 1/

P_2O_5 applied per acre	Reported yields per acre							
	Mitchell silt loam 2/				Minatare silt loam 3/			
	1931 4/	1932	1933	Total	1932 4/	1933	1934	Total
Pounds	Tons	Tons	Tons	Tons	Tons	Tons	Tons	Tons
0.0	4.73	5.26	5.14	15.13	2.31	2.52	2.46	7.29
31.5	5.57	5.98	5.46	17.01	3.59	2.87	2.86	9.32
45.0	5.67	6.18	5.79	17.64	3.93	3.37	2.83	10.13
67.5	5.45	6.33	5.61	17.39	4.37	3.56	3.42	11.35
90.0	5.64	6.59	5.88	18.11	4.41	3.80	4.23	12.44

1/ From Commercial Fertilizers for the Irrigated Sections of Western Nebraska (3).
2/ Designated as experiment 4 in the text.
3/ Designated as experiment 3 in the text.
4/ Year of application.

In both experiments double superphosphate was applied to established stands of alfalfa early in the spring. A grain drill with fertilizer attachment was used. The drill was set to disk the alfalfa lightly. Yields at all applied rates of P_2O_5 were substantially lower on the Minatare (experiment 3) than on the Mitchell soil (experiment 4), indicating the higher level of available phosphate in the latter.

The Utah Experiment

This experiment on Millville loam at North Logan, Utah, compares the effects of different kinds and rates of phosphate fertilizer on the yield of alfalfa hay. 7/ However, only the data from the double superphosphate rates are included here. The application was broadcast and harrowed into the soil when alfalfa was seeded alone in 1938. Yields of hay were reported in 1939, 1940, and 1941. The treatments were applied on small plots and replicated eight times in randomized blocks.

Table 7.- Reported yields of alfalfa at no application and at 2 rates of P_2O_5 applied as double superphosphate, North Logan, Utah

P_2O_5 applied per acre	Reported yields per acre 1939 1/	1940 1/	1941 2/	Total
Pounds	Tons	Tons	Tons	Tons
0	2.76	2.17	2.31	7.24
50	4.45	2.97	2.42	9.84
100	5.45	3.59	2.64	11.68

1/ From "Fertilizers for Utah Soils" (7).

2/ Unpublished data for 1941 supplied by D. W. Thorne, Utah Agricultural Experiment Station.

7/ Designated as experiment 5 in the text.

Table 15.- Values of $1-R^x$ when R = 0.8
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
0.00	------	000223	000446	000669	000892	001125	001338	001561	001784	002006
01	002229	002452	002674	002897	003119	003342	003564	003786	004009	004231
02	004453	004675	004897	005119	005341	005563	005785	006007	006228	006450
03	006672	006894	007115	007337	007558	007780	008001	008222	008444	008665
04	008886	009107	009328	009549	009770	009991	010212	010433	010654	010874
05	011095	011315	011536	011757	011977	012198	012418	012639	012859	013079
06	013299	013519	013740	013960	014180	014400	014620	014839	015059	015279
07	015499	015718	015938	016158	016377	016597	016816	017035	017254	017474
08	017693	017912	018131	018350	018569	018788	019007	019226	019445	019664
09	019883	020101	020320	020538	020757	020975	021194	021412	021631	021849
10	022067	022285	022503	022721	022940	023158	023376	023593	023811	024029
11	024247	024465	024683	024900	025118	025335	025553	025770	025987	026205
12	026422	026639	026856	027073	027290	027508	027725	027942	028158	028375
13	028592	028809	029026	029242	029459	029675	029892	030108	030325	030541
14	030757	030974	031190	031406	031622	031838	032054	032270	032486	032702
15	032918	033133	033349	033565	033780	033996	034212	034427	034642	034858
16	035073	035288	035504	035719	035934	036149	036364	036579	036794	037009
17	037224	037439	037654	037868	038083	038298	038512	038726	038941	039156
18	039370	039584	039799	040013	040227	040441	040655	040869	041083	041297
19	041511	041725	041939	042153	042366	042580	042794	043007	043220	043434
20	043648	043861	044074	044288	044501	044714	044927	045140	045353	045566
21	045779	045992	046205	046418	046631	046843	047055	047268	047481	047794
22	047906	048119	048331	048543	048755	048968	049180	049392	049604	049816
23	050028	050240	050452	050664	050876	051088	051298	051511	051723	051934
24	052145	052357	052569	052780	052991	053203	053414	053625	053836	054047
25	054258	054469	054680	054891	055102	055313	055524	055735	055945	056156
26	056366	056577	056787	056998	057208	057419	057629	057839	058049	058260
27	058470	058680	058890	059100	059310	059520	059729	059939	060149	060358
28	060568	060778	060987	061197	061406	061616	061825	062035	062244	062453
29	062662	062872	063081	063290	063499	063707	063916	064125	064334	064543
30	064752	064960	065169	065377	065586	065794	066003	066211	066420	066628
31	066836	067044	067253	067461	067669	067877	068085	068293	068500	068708
32	068916	069124	069332	069540	069747	069954	070162	070369	070577	070784
33	070992	071199	071406	071613	071820	072027	072234	072441	072648	072855
34	073062	073269	073476	073683	073889	074096	074302	074509	074715	074921
35	075128	075335	075541	075747	075953	076160	076366	076572	076778	076984
36	077190	077396	077602	077807	078013	078219	078424	078630	078836	079041
37	079247	079452	079658	079863	080068	080273	080478	080684	080889	081094
38	081299	081504	081709	081914	082119	082323	082528	082732	082937	083142
39	083347	083551	083756	083960	084165	084369	084573	084777	084982	085186
40	085390	085594	085798	086002	086206	086310	086613	086817	087021	087225
41	087429	087632	087836	088039	088243	088446	088649	088853	089056	089259
42	089463	089666	089869	090072	090275	090478	090681	090884	091086	091289
43	091492	091695	091898	092100	092303	092505	092708	092910	093113	093315
44	093517	093719	093922	094124	094326	094528	094730	094932	095134	095336
45	095538	095740	095941	096143	096345	096546	096748	096949	097151	097352
46	097554	097755	097956	098157	098359	098560	098761	098962	099163	099364
47	099565	099766	099967	100168	100369	100569	100770	100970	101171	101371
48	101572	101773	101973	102173	102374	102574	102774	102974	103175	103375
49	103575	103775	103975	104175	104374	104574	104774	104974	105173	105373
50	105573	105772	105972	106171	106371	106570	106770	106969	107168	107367
51	107567	107766	107965	108164	108363	108562	108760	108959	109158	109357
52	109556	109754	109953	110152	110350	110549	110747	110945	111143	111342
53	111540	111738	111937	112135	112333	112531	112729	112927	113125	113323
54	113521	113719	113916	114114	114312	114509	114707	114904	115102	115299
55	115497	115694	115891	116089	116286	116483	116680	116877	117074	117271
56	117468	117665	117862	118059	118256	118452	118649	118846	119042	119239
57	119435	119632	119828	120024	120220	120417	120614	120810	121006	121202
58	121398	121594	121790	121986	122182	122378	122574	122769	122965	123160
59	123356	123552	123748	123943	124138	124334	124529	124725	124920	125115

- Continued -

Table 15.- Values of $1-R^x$ when $R = 0.8$ - Continued -
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
0.60	125310	125505	125701	125896	126091	126286	126481	126676	126870	127065
61	127260	127455	127649	127844	128039	128233	128428	128622	128817	129011
62	129206	129400	129594	129788	129982	130176	130370	130564	130758	130952
63	131146	131340	131534	131728	131921	132115	132308	132502	132696	132889
64	133083	133276	133470	133663	133856	134050	134243	134436	134629	134822
65	135015	135208	135401	135594	135787	135980	136172	136365	136558	136750
66	136943	137136	137328	137521	137713	137906	138098	138290	138483	138675
67	138867	139059	139251	139443	139635	139827	140019	140211	140403	140595
68	140786	140978	141170	141361	141553	151744	141936	142127	142319	142510
69	142701	142893	143084	143275	143466	143657	143848	144039	144230	144421
70	144612	144803	144994	145185	145376	145566	145757	145947	146138	146328
71	146519	146709	146900	147090	147280	147471	147661	147851	148041	148231
72	148421	148611	148801	148991	149181	149371	149561	149750	149940	150130
73	150319	150509	150698	150888	151077	151267	151456	151645	151835	152024
74	152213	152403	152592	152781	152970	153159	153348	153536	153725	153914
75	154103	154292	154480	154669	154858	155046	155235	155423	155612	155800
76	155988	156177	156365	156553	156741	156930	157118	157306	157494	157682
77	157870	158058	158245	158433	158621	158809	158997	159184	159372	159559
78	159747	159934	160122	160309	160497	160684	160871	161058	161245	161433
79	161620	161807	161994	162181	162368	162555	162741	162928	163115	163302
80	163488	163675	163862	164048	164235	164421	164607	164794	164980	165167
81	165353	165539	165725	165912	166098	166284	166470	166656	166841	167027
82	167213	167399	167585	167771	167956	168142	168327	168513	168698	168884
83	169070	169255	169440	169625	169811	169996	170181	170366	170552	170737
84	170922	171107	171292	171476	171661	171846	172031	172216	172400	172585
85	172770	172954	173139	173323	173508	173692	173876	174061	174245	174429
86	174614	174798	174982	175166	175350	175534	175718	175902	176085	176269
87	176453	176637	176821	177004	177188	177371	177555	177738	177922	178105
88	178289	178472	178655	178839	179022	179205	179388	179571	179754	179937
89	180120	180303	180486	180669	180852	181035	181217	181400	181583	181765
90	181948	182130	182313	182495	182678	182860	183042	183225	183407	183589
91	183771	183953	184135	184317	184499	184681	184863	185045	185227	185409
92	185591	185772	185954	186136	186317	186499	186680	186862	187043	187225
93	187406	187587	187768	187950	188131	188312	188493	188674	188855	189036
94	189217	189398	189579	189760	189940	190121	190302	190483	190663	190844
95	191024	191205	191385	191566	191746	191926	192107	192287	192467	192647
96	192827	193008	193188	193368	193548	193728	193907	194087	194267	194447
97	194627	194806	194986	195166	195345	195525	195704	195884	196063	196242
98	196422	196601	196780	196960	197139	197318	197497	197676	197855	198034
99	198213	198392	198571	198750	198928	199107	199286	199464	199643	199821
1.00	200000	200179	200357	200535	200714	200892	201070	201249	201427	201605
01	201783	201961	202139	202317	202495	202673	202851	203029	203207	203385
02	203563	203740	203918	204095	204273	204451	204628	204805	204983	205160
03	205338	205515	205692	205869	206047	206224	206401	206578	206755	206932
04	207109	207286	207463	207640	207816	207993	208170	208346	208523	208700
05	208876	209053	209229	209406	209582	209758	209935	210111	210287	210463
06	210640	210816	210992	211168	211344	211520	211696	211872	212047	212223
07	212399	212575	212750	212926	213102	213277	213453	213628	213804	213979
08	214154	214330	214505	214680	214856	215031	215206	215381	215556	215731
09	215906	216081	216256	216431	216606	216780	216955	217130	217304	217479
1.10	217654	217828	218003	218177	218352	218526	218700	218875	219049	219223
11	219398	219572	219746	219920	220094	220268	220442	220616	220790	220964
12	221138	221311	221485	221659	221832	222006	222180	222353	222526	222700
13	222874	223047	223220	223394	223567	223740	223913	224086	224260	224433
14	224606	224779	224952	225125	225298	225470	225643	225816	225989	226161
15	226334	226507	226679	226852	227024	227197	227369	227542	227714	227886
16	228059	228231	228403	228575	228747	228919	229091	229263	229435	229607
17	229779	229951	230123	230295	230466	230638	230810	230981	231153	231324
18	231496	231667	231839	232010	232182	232353	232524	232695	232867	233038
19	233209	233380	233551	233722	233893	234064	234235	234406	234577	234747

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8 - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
1.20	234918	235089	235260	235430	235601	235771	235942	236112	236282	236453
21	236623	236794	236964	237134	237304	237475	237645	237815	237985	238155
22	238325	238495	238665	238835	239004	239174	239344	239513	239683	239853
23	240023	240192	240362	240531	240701	240870	241039	241209	241378	241547
24	241717	241886	242055	242224	242393	242562	242731	242900	243069	243238
25	243407	243576	243744	243913	244082	244250	244419	244588	244756	244925
26	245093	245262	245430	245598	245767	245935	246103	246271	246440	246608
27	246776	246944	247112	247280	247448	247616	247784	247951	248119	248287
28	248455	248622	248790	248958	249125	249293	249460	249628	249795	249963
29	250130	250297	250464	250632	250799	250966	251133	251300	251467	251634
30	251801	251968	252135	252302	252469	252635	252802	252969	253135	253302
31	253469	253635	253802	253968	254135	254301	254468	254634	254800	254967
32	255133	255299	255465	255631	255797	255963	256130	256296	256461	256627
33	256793	256959	257125	257291	257456	257622	257788	257953	258119	258284
34	258450	258615	258781	258946	259111	259277	259442	259607	259772	259938
35	260103	260268	260433	260598	260763	260928	261093	261257	261422	261587
36	261752	261917	262081	262246	262410	262575	262740	262904	263068	263233
37	263397	263562	263726	263890	264055	264219	264383	264547	264711	264875
38	265039	265203	265367	265531	265695	265859	266022	266186	266350	266514
39	266677	266841	267005	267168	267332	267495	267659	267822	267985	268149
40	268312	268475	268638	268801	268964	269128	269291	269454	269617	269780
41	269943	270106	270269	270431	270594	270757	270920	271082	271245	271407
42	271570	271733	271895	272057	272220	272382	272545	272707	272869	273031
43	273194	273356	273518	273680	273842	274004	274166	274328	274490	274652
44	274814	274976	275137	275299	275461	275622	275784	275945	276107	276269
45	276430	276592	276753	276914	277076	277237	277398	277559	277721	277882
46	278043	278204	278365	278526	278687	278848	279009	279170	279331	279491
47	279652	279813	279973	280134	280295	280455	280616	280776	280937	281097
48	281258	281418	281578	281739	281899	282059	282219	282380	282540	282700
49	282860	283020	283180	283340	283500	283660	283819	283979	284139	284299
50	284458	284618	284777	284937	285097	285256	285415	285575	285734	285894
51	286053	286212	286372	286531	286690	286849	287008	287167	287326	287486
52	287644	287803	287962	288121	288280	288439	288598	288756	288915	289074
53	289232	289391	289550	289708	289867	290025	290183	290342	290500	290658
54	290816	290975	291133	291291	291449	291607	291765	291923	292081	292239
55	292397	292555	292713	292871	293029	293186	293344	293502	293659	293817
56	293975	294132	294290	294447	294604	294762	294919	295077	295234	295391
57	295548	295706	295863	296020	296177	296334	296491	296648	296805	296962
58	297118	297275	297432	297589	297746	297902	298059	298216	298372	298528
59	298685	298841	298998	299154	299311	299467	299623	299780	299936	300093
60	300249	300405	300561	300717	300873	301029	301185	301341	301496	301652
61	301808	301964	302119	302275	302431	302587	302742	302898	303053	303209
62	303364	303520	303675	303830	303986	304141	304296	304452	304607	304762
63	304917	305072	305227	305382	305537	305692	305847	306002	306157	306312
64	306466	306621	306776	306931	307085	307240	307394	307549	307703	307858
65	308012	208166	308321	308475	308629	308784	308938	309092	309246	309401
66	309555	309709	309863	310017	310171	310325	310478	310632	310786	310940
67	311093	311247	311401	311555	311708	311862	312015	312169	312322	312476
68	312629	312782	312936	313089	313242	313396	313549	313702	313855	314008
69	314161	314314	314467	314620	314773	214926	315079	315232	315385	315537
70	315690	315843	315995	316148	316300	316453	316605	316758	316910	317063
71	317215	317367	317520	317672	317824	317977	318129	318281	318433	318585
72	318737	318889	319041	319193	319345	319497	319648	319800	319952	320104
73	320256	320407	320559	320711	320862	321014	321165	321317	321468	321619
74	321771	321923	322074	322225	322376	322527	322678	322829	322980	323131
75	323282	323433	323584	323735	323886	324037	324188	324339	324489	324640
76	324791	324941	325092	325243	325393	325544	325694	325845	325995	326145
77	326296	326446	326596	326746	326897	327047	327197	327347	327497	327648
78	327798	327947	328097	328247	328397	328547	328697	328847	328997	329146
79	329296	329445	329595	329744	329894	330044	330193	330343	330492	330641

- Continued -

Table 15.- Values of $1-R^x$ when $R = 0.8$ - Continued -
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
1.80	330791	330940	331089	331238	331388	331537	331686	331835	331984	332133
81	332282	332431	332580	332729	332878	333027	333176	333325	333474	333622
82	333771	333919	334068	334217	334365	334514	334762	334810	334959	335107
83	335256	335404	335552	335701	335849	335997	336145	336293	336441	336589
84	336737	336885	337033	337181	337329	337477	337625	337773	337920	338068
85	338216	338363	338511	338659	338806	338954	339101	339249	339396	339543
86	339691	339838	339985	340133	340280	340427	340574	340721	340868	341015
87	341163	341310	341457	341604	341750	341897	342044	342191	342338	342484
88	342631	342778	342924	343071	343218	343364	343511	343657	343803	343950
89	344096	344243	344389	344535	344681	344828	344974	345120	345266	345412
90	345558	345704	345850	345996	346142	346288	346434	346580	346726	346872
91	347017	347163	347308	347454	347600	347745	347891	348036	348182	348327
92	348472	348618	348763	348909	349054	349199	349344	349489	349634	349780
93	349925	350070	350215	350360	350505	350650	350794	350939	351084	351229
94	351374	351518	351663	351808	351952	352097	352241	352385	322530	352675
95	352820	352964	353108	353252	353397	353541	353685	353829	353974	354118
96	354262	354406	354550	354694	354838	354982	355126	355270	355414	355558
97	355701	355845	355989	356132	356276	356420	356563	356707	356851	356994
98	357137	357281	357424	357568	357711	357854	357998	358141	358284	358427
99	358570	358713	358856	359000	359143	359286	359428	359571	359714	359857
2.00	360000	360143	360285	360428	360571	360714	360856	360999	361141	361284
01	361426	361569	361711	361854	361996	362139	362281	362423	362565	362708
02	362850	362992	363134	363276	363418	363560	363702	363844	363986	364128
03	364270	364412	364554	364695	364837	364979	365121	365262	365404	365545
04	365687	365829	365970	366112	366253	366394	366536	366677	366818	366960
05	367101	367242	367383	367525	367666	367807	367948	368089	368230	368371
06	368512	368652	368793	368934	369075	369216	369357	369497	369638	369778
07	369919	370060	370200	370341	370481	370622	370762	370903	371043	371183
08	371323	371464	371604	371744	371884	372025	372165	372305	372445	372585
09	372725	372865	373005	373145	373285	373424	373564	373704	373844	373983
10	374123	374263	374402	374542	374681	374821	374960	375100	375240	375379
11	375518	375657	375797	375936	376075	376214	376354	376493	376632	376771
12	376910	377049	377188	377327	377466	377605	377744	377882	378021	378160
13	378299	378438	378576	378715	378854	378992	379131	379269	379408	379546
14	379685	379823	379961	380100	380238	380376	380515	380653	380791	380929
15	381067	381205	381343	381481	381619	381757	381895	382033	382171	382309
16	382447	382585	382722	382860	382998	383135	383273	383411	383548	383686
17	383823	383961	384098	384236	384373	384510	384648	384785	384922	385060
18	385197	385334	385471	385608	385745	385882	386019	386156	386293	386430
19	386567	386704	386841	386978	387114	387251	387388	387524	387661	387798
20	387934	388071	388207	388344	388480	388617	388753	388889	389026	389162
21	389299	389435	389571	389707	389843	389980	390116	390252	390388	390524
22	390660	390796	390932	391068	391204	391339	391475	391611	391747	391883
23	392018	392154	392289	392425	392561	392696	392831	392967	393102	393238
24	393373	393509	393644	393779	393914	394050	394185	394320	394455	394590
25	394725	394860	394995	395130	395265	395400	395535	395670	395805	395940
26	396075	396209	396344	396479	396614	396748	396883	397017	397151	397286
27	397421	397555	397689	397824	397958	398093	398227	398361	398495	398630
28	398764	398898	399032	399166	399300	399434	399568	399702	399836	399970
29	400104	400238	400372	400505	400639	400773	400907	401040	401174	401307
30	401441	401574	401708	401842	401975	402108	402242	402375	402509	402642
31	402775	402908	403042	403175	403308	403441	403574	403707	403840	403973
32	404106	404239	404372	404505	404638	404771	404904	405036	405169	405302
33	405435	405567	405700	405832	405964	406097	406230	406362	406495	406627
34	406760	406892	407025	407157	407289	407421	407553	407686	407818	407950
35	408082	408214	408346	408478	408610	408742	408874	409006	409138	409270
36	409401	409533	409665	409797	409928	410060	410192	410323	410455	410586
37	410718	410849	410981	411112	411244	411375	311506	411638	411769	411900
38	412031	412163	412294	412425	412556	412687	412818	412949	413080	413211
39	413342	413473	413604	413734	413865	413996	414127	414258	414388	414519

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8 - Continued -
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
2.40	414650	414780	414911	415041	415172	415302	415433	415563	415694	415824
41	415954	416085	416215	416345	416475	416606	416736	416866	416996	417126
42	417256	417386	417516	417646	417776	417906	418036	418166	418295	418425
43	418555	418685	418814	418944	419074	419203	419333	419463	419592	419721
44	419851	419980	420110	420239	420369	420498	420627	420756	420886	421015
45	421144	421273	421402	421531	421660	421790	421919	422048	422177	422306
46	422434	422563	422692	422821	422950	423078	423207	423336	423465	423593
47	423722	423850	423979	424107	424236	424364	424493	424621	424750	424878
48	425006	425134	425263	425391	425519	425647	425775	425904	426032	426160
49	426288	426416	426544	426672	426800	426928	427055	427183	427311	427439
50	427567	427694	427822	427950	428077	428205	428332	428460	428588	428715
51	428843	428970	429097	429225	429352	429479	429607	429734	429861	429988
52	430116	430243	430370	430497	430624	430751	430878	431005	431132	431259
53	431386	431513	431640	431766	431893	432020	432147	432273	432400	432527
54	432653	432780	432906	433033	433159	433286	433412	433539	433665	433792
55	433918	434044	434170	434297	434423	434549	434675	434801	434928	435054
56	435180	435306	435432	435558	435684	435809	435935	436061	436187	436313
57	436439	436564	436670	436816	436941	437067	437193	437318	437444	437569
58	437695	437820	437946	438071	438197	438322	438447	438572	438698	438823
59	438948	439073	439198	439323	439448	439574	439699	439824	439949	440074
60	440199	440323	440448	440573	440698	440823	440948	441072	441197	441322
61	441446	441571	441696	441820	441945	442069	442194	442318	442443	442567
62	442691	442816	442940	443064	443189	443313	443437	443561	443685	443809
63	443933	444058	444182	444306	444430	444554	444678	444801	444925	445049
64	445173	445297	445420	445544	445668	445792	445915	446039	446163	446286
65	446410	446533	446657	446780	446904	447027	447150	447274	447397	447520
66	447644	447767	447890	448013	448136	448260	448383	448506	448629	448752
67	448875	448998	449121	449244	449367	449489	449612	449735	449858	449981
68	450103	450226	450349	450471	450594	450716	450839	450962	451084	451207
69	451329	451451	451574	451696	451818	451941	452063	452175	452308	452430
70	452552	452674	452796	452918	453040	453162	453284	453406	453528	453650
71	453772	453894	454016	454138	454259	454381	454503	454625	454746	454868
72	454990	455111	455233	455354	455476	455597	455719	455840	455962	456083
73	456204	456326	456447	456568	456690	456811	456932	457053	457174	457295
74	457416	457538	457659	457780	457901	458022	458142	458263	458384	458505
75	458626	458747	458867	458988	459109	459230	459350	459471	459592	459712
76	459833	459953	460074	460194	460315	460435	460555	460676	460796	460916
77	461037	461157	461277	461397	461517	461638	461758	461878	461998	462118
78	462238	462358	462478	462598	462718	462838	462958	463077	463197	463317
79	463437	463556	463676	463795	463915	464035	464155	464274	464394	464513
80	464633	464752	464871	464991	465110	465230	465349	465468	465587	465707
81	465826	465945	466064	466183	466302	466422	466541	466660	466779	466898
82	467017	467135	467254	467373	467492	467611	467730	467848	467967	468086
83	468205	468323	468442	468560	468679	468798	468916	469035	469153	469272
84	469390	469508	469627	469745	469863	469981	470100	470218	470336	470454
85	470573	470691	470809	470927	471045	471163	471281	471399	471517	471635
86	471753	471871	471988	472106	472224	472342	472460	472577	472695	472812
87	472930	473048	473165	473283	473400	473518	473635	473753	473870	473988
88	474105	474222	474339	474457	474574	474681	474808	474926	475043	475160
89	475277	475394	475511	475628	475745	475862	475979	476096	476213	476330
90	476447	476563	476680	476797	476914	477030	477147	477264	477380	477497
91	477614	477730	477847	477963	478080	478196	478312	478429	478545	478662
92	478778	478894	479011	479127	479243	479359	479475	479592	479708	479824
93	479940	480056	480172	480288	480404	480520	480636	480751	480867	480983
94	481099	481215	481331	481446	481562	481678	481793	481909	482025	482140
95	482256	482371	482487	482602	482717	482833	482948	483064	483179	483294
96	483410	483525	483640	483755	483871	483986	484101	484216	484331	484446
97	484561	484676	484791	484906	485021	485136	485251	485365	485480	485595
98	485710	485825	485939	486054	486169	486284	486398	486513	486627	486742
99	486856	486971	487085	487200	487314	487428	487543	487657	487772	487886

- Continued -

Table 15.- Values of $1-R^x$ when $R = 0.8$ - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
3.00	488000	488114	489228	488343	488457	488571	488685	488799	488913	489027
01	489141	489255	489369	489483	489597	489711	489825	489939	490052	490166
02	490280	490394	490507	490621	490735	490848	490961	491075	491189	491303
03	491416	491530	491643	491757	491870	491983	492096	492210	492323	492436
04	492550	492663	492776	492889	493002	493115	493229	493342	493455	493568
05	493681	493794	493907	494020	494132	494245	494358	494471	494584	494697
06	494809	494922	495035	495147	495260	495373	495485	495598	495710	495823
07	495935	496048	496160	496273	496385	496497	496610	496722	496834	496947
08	497059	497171	497283	497395	497508	497620	497732	497844	497956	498068
09	498180	498292	498404	498516	498628	498740	498851	498963	499075	499187
10	499298	499410	499522	499633	499745	499857	499968	500080	500191	500303
11	500414	500526	500637	500749	500860	500971	501083	501194	501305	501417
12	501528	501639	501750	501862	501973	502084	502195	502306	502417	502528
13	502639	502750	502861	502972	503083	503194	503305	503415	503526	503637
14	503748	503858	503969	504080	504190	504301	504412	504522	504633	504743
15	504854	504964	505075	505185	505296	505406	505516	505627	505737	505847
16	505958	506068	506178	506288	506398	506508	506618	506729	506839	506949
17	507059	507169	507279	507389	507498	507608	507718	507828	507938	508048
18	508157	508267	508377	508486	508596	508706	508815	508925	509035	509144
19	509254	509363	509473	509582	509691	509801	509910	510020	510129	510238
20	510348	510457	510566	510675	510784	510893	511003	511112	511221	511330
21	511439	511548	511657	511766	511875	511984	512093	512202	512310	512419
22	512528	512637	512745	512854	512963	513072	513180	513289	513397	513506
23	513615	513723	513831	513940	514048	514157	514265	514374	514482	514590
24	514699	514807	514915	515024	515132	515240	515348	515456	515564	515672
25	515780	515888	515996	516104	516212	516320	516428	516536	516644	516752
26	516860	516967	517075	517183	517291	517398	517506	517614	517721	517829
27	517936	518044	518152	518259	518367	518474	518582	518689	518796	518904
28	519011	519118	519226	519333	519440	519547	519654	519762	519869	519976
29	520083	520190	520297	520404	520511	520618	520725	520832	520939	521046
30	521153	521260	521366	521473	521580	521687	521794	521900	522007	522114
31	522220	522327	522433	522540	522646	522753	522859	522966	523072	523178
32	523285	523392	523498	523604	523710	523817	523923	524029	524135	524242
33	524348	524454	524560	524666	524772	524878	524984	525090	525196	525302
34	525408	525514	525620	525725	525831	525937	526043	526148	526254	526360
35	526466	526572	526677	526783	526888	526994	527099	527205	527310	527416
36	527521	527627	527732	527837	527943	528048	528154	528259	528364	528469
37	528574	528680	528785	528890	528995	529100	529205	529310	529415	529520
38	529625	529730	529835	529940	530045	530150	530255	530359	530464	530569
39	530674	530778	530883	530987	531092	531197	531302	531406	531511	531615
40	531720	531824	531929	532033	532137	532242	532346	532451	532555	532659
41	532763	532868	532972	533076	533180	533284	533389	533493	533597	533701
42	533805	533909	534013	534117	534221	534325	534429	534532	534636	534740
43	534844	534948	535052	535155	535259	535363	535466	535570	535674	535777
44	535881	535984	536088	536191	536295	536398	536502	536605	536709	536812
45	536915	537019	537122	537225	537328	537432	537535	537638	537741	537844
46	537947	538050	538154	538257	538360	538463	538566	538669	538772	538874
47	538977	539080	539183	539286	539389	539491	539594	539697	539800	539902
48	540005	540108	540210	540313	540415	540518	540620	540723	540826	540928
49	541030	541133	541235	541337	541440	541542	541644	541747	541849	541951
50	542053	542155	542258	542360	542462	542564	542666	542768	542870	542972
51	543074	543176	543278	543380	543482	543584	543685	543787	543889	543991
52	544092	544194	544296	544398	544499	544601	544702	544804	544906	545007
53	545109	545210	545312	545413	545515	545616	545717	545819	545920	546021
54	546123	546224	546325	546426	546528	546629	546730	546831	546932	547033
55	547134	547235	547336	547437	547538	547639	547740	547841	547942	548043
56	548144	548245	548345	548446	548547	548648	548748	548849	548950	549050
57	549151	549251	549352	549453	549553	549654	549754	549855	549955	550056
58	550156	550256	550357	550457	550557	550657	550758	550858	550958	551058
59	551158	551259	551359	551459	551559	551659	551759	551859	551959	552059

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8 - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
3.60	552159	552259	552359	552459	552558	552658	552758	552858	552958	553057
61	553157	553257	553356	553456	553556	553655	553755	553855	553954	554054
62	554153	554253	554352	554451	554551	554650	554750	554849	554948	555047
63	555147	555246	555345	555445	555544	555643	555742	555841	555940	556039
64	556138	556237	556336	556435	556534	556633	556732	556831	556930	557029
65	557128	557227	557325	557424	557523	557622	557720	557819	557917	558016
66	558115	558214	558313	558411	558509	558608	558706	558805	558903	559001
67	559100	559198	559297	559395	559493	559591	559690	559788	559886	559984
68	560082	560181	560279	560377	560475	560573	560671	560769	560867	560965
69	561063	561161	561259	561357	561455	561553	561650	561748	561846	561944
70	562041	562139	562237	562335	562432	562530	562627	562725	562823	562920
71	563018	563115	563213	563310	563408	563505	563602	563700	563797	563894
72	563992	564089	564186	564284	564381	564478	564575	564672	564769	564866
73	564964	565061	556158	565255	565352	565449	565546	565643	565739	565836
74	565933	566030	566127	566224	566320	566417	566514	566611	566707	566804
75	566901	566997	567094	567191	567287	567384	567480	567577	567673	567770
76	567866	567963	568059	568155	568252	568348	568444	568541	568637	568733
77	568829	568925	569022	569118	569214	569310	569406	569502	569598	569694
78	569790	569886	569982	570078	570174	570270	570366	570462	570558	570654
79	570749	570845	570941	571037	571132	571228	571324	571419	571515	571610
80	571706	571802	571897	571993	572088	572184	572279	572374	572470	572565
81	572661	572756	572851	572947	573042	573137	573232	573328	573423	573518
82	573613	573708	573803	573899	573994	574089	574184	574279	574374	574469
83	574564	574659	574753	574848	574943	575038	575133	575228	575322	575417
84	575512	575607	575701	575796	575891	575985	576080	576174	576269	576363
85	576458	576552	576647	576741	576836	576931	577025	577119	577213	577308
86	577402	577496	577591	577685	577779	577873	577967	578062	578156	578250
87	578344	578438	578532	578626	578720	578814	578908	579002	579096	579190
88	579284	579378	579472	579565	579659	579753	579847	579941	580034	580128
89	580222	580315	580409	580502	580596	580690	580783	580877	580970	581064
90	581157	581251	581344	581438	581531	581624	581718	581811	581904	581998
91	582091	582184	582277	582370	582464	582557	582650	582743	582836	582929
92	583022	583115	583208	583301	583394	583487	583580	583673	583766	583859
93	593952	584045	584137	584230	584323	584416	584508	584601	584694	584787
94	584879	584972	585064	585157	585249	585342	585435	585527	585619	585712
95	585804	585897	585989	586082	586174	586266	586359	586451	586543	586635
96	586728	586820	586912	587004	587096	587189	587281	587373	587465	587557
97	587649	587741	587833	587925	588017	588109	588201	588292	588384	588476
98	588568	588660	588751	588843	588935	589027	589118	589210	589302	589393
99	589485	589577	589668	589760	589851	589943	590034	590126	590217	590309

Table 15.- Values of $1-R^x$ when $R = 0.8$ - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
4.0	59040	59131	59222	59313	59404	59494	59585	59675	59765	59854
1	59944	60033	60122	50211	60300	60388	60477	60565	60653	60740
2	60828	60915	61002	61089	61176	61262	61349	61435	61521	61607
3	61692	61778	61863	61948	62033	62117	62202	62286	62370	62454
4	62538	62621	62704	62787	62870	62953	63036	63118	63200	63282
5	63364	63446	63527	63609	63690	63771	63851	63932	64012	64093
6	64173	64253	64332	64412	64491	64570	64649	64728	64807	64885
7	64963	65041	65119	65197	65275	65352	65429	65506	65583	65660
8	65736	65813	65889	65965	66041	66117	66192	66268	66343	66418
9	66493	66567	66642	66716	66790	66864	66938	67012	67085	67159
5.0	67232	67305	67378	67451	67523	67596	67668	67740	67812	67883
1	67955	68027	68098	68169	68240	68311	68381	68451	68522	68592
2	68662	68732	68802	68871	68941	69010	69079	69148	69217	69285
3	69354	69422	69490	69558	69626	69694	69761	69829	69896	69963
4	70030	70097	70164	70230	70296	70363	70429	70495	70560	70626
5	70691	70757	70822	70887	70952	71016	71081	71146	71210	71274
6	71338	71402	71466	71529	71592	71656	71719	71782	71845	71908
7	71971	72033	72095	72158	72220	72282	72344	72406	72467	72528
8	72589	72650	72711	72772	72833	72893	72954	73014	73074	73134
9	73194	73254	73313	73373	73432	73491	73551	73610	73668	73727
6.0	73786	73844	73902	73960	74018	74076	74134	74192	74249	74307
1	74364	74421	74478	74535	74592	74649	74705	74761	74818	74874
2	74930	74986	75041	75097	75153	75208	75263	75318	75373	75428
3	75483	75538	75592	75647	75701	75755	75809	75863	75917	75970
4	76024	76077	76131	76184	76237	76290	76343	76396	76448	76501
5	76553	76605	76658	76710	76761	76813	76865	76917	76968	77019
6	77071	77122	77173	77224	77274	77325	77375	77426	77476	77526
7	77576	77626	77676	77726	77776	77825	77875	77924	77973	78022
8	78071	78120	78169	78218	78266	78315	78363	78411	78459	78507
9	78555	78603	78651	78698	78746	78793	78840	78888	78935	78982
7.0	79028	79075	79122	79168	79215	79261	79307	79354	79400	79445
1	79491	79537	79583	79628	79674	79719	79764	79809	79854	79899
2	79944	79989	80033	80078	80122	80166	80211	80255	80299	80343
3	80386	80430	80474	80517	80561	80604	80647	80690	80733	80776
4	80819	80862	80905	80947	80990	81032	81074	81117	81159	81201
5	81242	81284	81326	81367	81409	81451	81492	81533	81574	81615
6	81656	81697	81738	81779	81819	81860	81900	81941	81981	82021
7	82061	82101	82141	82181	82221	82260	82300	82339	82379	82418
8	82457	82496	82535	82574	82613	82652	82690	82729	82768	82806
9	82844	82882	82920	82959	82997	83035	83072	83110	83148	83185
8.0	83223	83260	83297	83335	83372	83409	83446	83483	83520	83557
1	83593	83630	83666	83702	83739	83775	83811	83847	83883	83919
2	83955	83991	84027	84062	84098	84133	84168	84204	84239	84274
3	84309	84344	84379	84414	84449	84483	84518	84552	84587	84621
4	84655	84690	84724	84758	84792	84826	84859	84893	84927	84960
5	84994	85027	85061	85094	85127	85161	85194	85227	85259	85292
6	85325	85358	85391	85423	85456	85488	85520	85552	85585	85617
7	85649	85681	85713	85745	85776	85808	85840	85872	85903	85934
8	85966	85997	86028	86059	86090	86121	86152	86183	86214	86245
9	86274	86305	86336	86367	86397	86428	86458	86488	86518	86548
9.0	86578	86608	86638	86668	86697	86727	86757	86786	86816	86845
1	86875	86904	86933	86962	86991	87020	87049	87078	87107	87136
2	87164	87193	87221	87250	87278	87306	87335	87363	87391	87419
3	87447	87475	87503	87531	87559	87587	87614	87642	87669	87697
4	87724	87752	87779	87806	87833	87860	87887	87915	87942	87968
5	87995	88022	88049	88075	88102	88128	88155	88181	88208	88234
6	88260	88286	88312	88338	88364	88390	88416	88442	88468	88494
7	88519	88545	88570	88596	88621	88647	88672	88697	88722	88747
8	88773	88798	88823	88847	88872	88897	88922	88947	88971	88996
9	89020	89045	89069	89094	89118	89142	89166	89190	89215	89239

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8 - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
10.0	89263	89287	89310	89334	89358	89382	89405	89429	89453	89476
.1	89500	89523	89546	89570	89593	89616	89639	89662	89685	89708
2	89731	89754	89777	89800	89822	89845	89868	89890	89913	89936
3	89958	89980	90003	90025	90047	90069	90091	90113	90135	90157
4	90179	90201	90223	90245	90267	90288	90310	90332	90353	90375
5	90396	90418	90439	90460	90482	90503	90524	90545	90566	90587
6	90608	90629	90650	90671	90692	90712	90733	90754	90774	90795
7	90815	90836	90856	90877	90897	90917	90937	90958	90978	90998
8	91018	91038	91058	91078	91098	91118	91138	91157	91177	91197
9	91216	91236	91255	91275	91294	91314	91333	91352	91372	91391
11.0	91410	91429	91448	91467	91486	91505	91524	91543	91562	91581
1	91600	91618	91637	91656	91674	91693	91711	91730	91748	91767
2	91785	91803	91822	91840	91858	91876	91894	91912	91930	91948
3	91966	91984	92002	92020	92038	92055	92073	92091	92108	92126
4	92144	92161	92179	92196	92213	92231	92248	92265	92283	92300
5	92317	92334	92351	92368	92385	92402	92419	92436	92453	92470
6	92487	92503	92520	92537	92553	92570	92586	92603	92619	92636
7	92652	92669	92685	92701	92718	92734	92750	92766	92782	92798
8	92814	92830	92846	92862	92878	92894	92910	92926	92942	92957
9	92973	92989	93004	93020	93035	93051	93066	93082	93097	93113
12.0	93128	93143	93159	93174	93189	93204	93219	93235	93250	93265
1	93280	93295	93310	93324	93339	93354	93369	93384	93399	93413
2	93428	93443	93457	93472	93486	93501	93515	93530	93544	93559
3	93573	93587	93602	93616	93630	93644	93658	93673	93687	93701
4	93715	93729	93743	93757	93771	93785	93798	93812	93826	93840
5	93853	93867	93881	93895	93908	93922	93935	93949	93962	93976
6	93989	94003	94016	94029	94043	94056	94069	94082	94095	94109
7	94122	94135	94148	94161	94174	94187	94200	94213	94226	94239
8	94252	94264	94277	94290	94303	94315	94328	94341	94353	94366
9	94378	94391	94403	94416	94428	94441	94453	94465	94478	94490
13.0	94502	94515	94527	94539	94551	94563	94575	94588	94600	94612
1	94624	94636	94648	94660	94671	94683	94695	94707	94719	94731
2	94742	94754	94766	94777	94789	94801	94812	94824	94835	94847
3	94858	94870	94881	94893	94904	94915	94927	94938	94949	94961
4	94972	94983	94994	95005	95017	95028	95039	95050	95061	95072
5	95083	95094	95105	95116	95126	95137	95148	95159	95170	95181
6	95191	95202	95213	95223	95234	95245	95255	95266	95276	95287
7	95297	95308	95318	95329	95339	95349	95360	95370	95381	95391
8	95401	95411	95422	95432	95442	95452	95462	95472	95483	95493
9	95503	95513	95523	95533	95543	95553	95563	95572	95582	95592
14.0	95602	95612	95621	95631	95641	95651	95660	95670	95680	95689
1	95699	95709	95718	95728	95737	95747	95756	95766	95775	95784
2	95794	95803	95813	95822	95831	95841	95850	95859	95868	95878
3	95887	95896	95905	95914	95923	95932	95941	95951	95960	95969
4	95978	95987	95995	96004	96013	96022	96031	96040	96049	96058
5	96066	96075	96084	96092	96101	96110	96119	96127	96136	96144
6	96153	96162	96170	96179	96187	96196	96204	96213	96221	96230
7	96238	96246	96255	96263	96271	96280	96288	96296	96304	96313
8	96321	96329	96337	96346	96354	96362	96370	96378	96386	96394
9	96402	96410	96418	96426	96434	96442	96450	96458	96466	96474
15.0	96482	96489	96497	96505	96513	96521	96528	96536	96544	96551
1	96559	96567	96574	96582	96590	96597	96605	96612	96620	96628
2	96635	96643	96650	96658	96665	96672	96680	96687	96695	96702
3	96709	96717	96724	96731	96739	96746	96753	96760	96768	96775
4	96782	96789	96796	96803	96811	96818	96825	96832	96839	96846
5	96853	96860	96867	96874	96881	96888	96895	96902	96909	96916
6	96923	96929	96936	96943	96950	96957	96963	96970	96977	96984
7	96991	96998	97004	97010	97017	97024	97030	97037	97044	97050
8	97057	97063	97070	97076	97083	97089	97096	97102	97109	97115
9	97122	97128	97135	97141	97147	97154	97160	97166	97173	97179

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8-Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
16.0	97185	97192	97198	97204	97210	97216	97223	97229	97235	97241
1	97247	97253	97260	97266	97272	97278	97284	97290	97296	97302
2	97308	97314	97320	97326	97332	97338	97344	97350	97356	97362
3	97368	97373	97379	97385	97391	97397	97403	97408	97414	97420
4	97426	97431	97437	97443	97448	97454	97460	97465	97471	97477
5	97482	97488	97494	97499	97505	97510	97516	97521	97527	97532
6	97538	97544	97549	97554	97560	97565	97571	97576	97581	97587
7	97592	97598	97603	97608	97614	97619	97624	97630	97635	97640
8	97645	97651	97656	97661	97666	97671	97677	97682	97687	97692
9	97697	97702	97708	97713	97718	97723	97728	97733	97738	97743
17.0	97748	97753	97758	97763	97768	97773	97778	97783	97788	97793
1	97798	97803	97808	97813	97817	97822	97827	97832	97837	97842
2	97846	97851	97856	97861	97866	97870	97875	97880	97885	97889
3	97894	97899	97903	97908	97913	97917	97922	97927	97931	97936
4	97940	97945	97950	97954	97959	97963	97968	97972	97977	97981
5	97986	97990	97995	97999	98004	98008	98013	98017	98022	98026
6	98030	98035	98039	98043	98048	98052	98056	98061	98065	98069
7	98074	98078	98082	98087	98091	98095	98099	98104	98108	98112
8	98116	98120	98125	98129	98133	98137	98141	98146	98150	98154
9	98158	98162	98166	98170	98174	98178	98182	98186	98190	98194
18.0	98199	98203	98207	98211	98215	98219	98223	98226	98230	98234
1	98238	98242	98246	98250	98254	98258	98262	98266	98269	98273
2	98277	98281	98285	98289	98292	98296	98300	98304	98308	98311
3	98315	98319	98323	98326	98330	98334	98338	98341	98345	98349
4	98352	98356	98360	98363	98367	98371	98374	98378	98382	98385
5	98389	98392	98396	98399	98403	98406	98410	98414	98417	98421
6	98424	98428	98431	98435	98438	98442	98445	98449	98452	98456
7	98459	98462	98466	98469	98472	98476	98480	98483	98486	98490
8	98494	98497	98500	98503	98506	98510	98513	98516	98520	98523
9	98526	98530	98533	98536	98539	98543	98546	98549	98552	98556
19.0	98559	98562	98565	98568	98572	98575	98578	98581	98584	98587
1	98591	98594	98597	98600	98603	98606	98609	98612	98616	98619
2	98622	98625	98628	98631	98634	98637	98640	98643	98646	98649
3	98652	98655	98658	98661	98664	98667	98670	98673	98676	98679
4	98682	98685	98688	98691	98694	98697	98699	98702	98705	98708
5	98711	98714	98717	98720	98722	98725	98728	98731	98734	98737
6	98739	98742	98745	98748	98751	98753	98756	98759	98762	98765
7	98767	98770	98773	98775	98778	98781	98784	98786	98789	98792
8	98794	98797	98800	98802	98805	98808	98810	98813	98816	98819
9	98821	98824	98826	98829	98832	98834	98837	98839	98842	98845
20.0	98847	98850	98852	98855	98857	98860	98862	98865	98867	98870
1	98873	98876	98878	98880	98883	98885	98888	98890	98892	98895
2	98897	98900	98902	98905	98907	98910	98912	98914	98917	98919
3	98922	98924	98927	98929	98931	98934	98936	98938	98941	98943
4	98945	98948	98950	98953	98955	98957	98960	98962	98964	98966
5	98969	98971	98973	98976	98978	98980	98982	98985	98988	98990
6	98992	98994	98996	98998	99001	99003	99005	99007	99009	99012
7	99014	99016	99018	99020	99023	99025	99027	99029	99031	99034
8	99036	99038	99040	99042	99044	99046	99048	99051	99053	99055
9	99057	99059	99061	99063	99065	99067	99069	99071	99073	99075
21.0	99077	99080	99082	99084	99086	99088	99090	99092	99094	99096
1	99098	99100	99102	99104	99106	99108	99110	99112	99114	99116
2	99118	99120	99122	99124	99126	99128	99130	99132	99134	99136
3	99137	99139	99141	99143	99145	99147	99149	99151	99153	99155
4	99157	99158	99160	99162	99164	99166	99168	99170	99171	99173
5	99175	99177	99179	99181	99182	99184	99186	99188	99190	99192
6	99193	99195	99197	99199	99201	99202	99204	99206	99208	99209
7	99211	99213	99215	99216	99218	99220	99222	99223	99225	99227
8	99229	99230	99232	99234	99235	99237	99239	99241	99242	99244
9	99246	99247	99249	99251	99252	99254	99256	99257	99259	99261

- Continued -

Table 15.- Values of $1-R^x$ when $R = 0.8$ - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
22.0	99262	99264	99266	99267	99269	99270	99272	99274	99275	99277
1	99279	99280	99282	99283	99285	99286	99288	99290	99291	99293
2	99294	99296	99298	99299	99300	99302	99304	99305	99307	99308
3	99310	99312	99313	99315	99316	99318	99319	99321	99322	99324
4	99325	99327	99328	99330	99331	99333	99334	99336	99338	99339
5	99340	99341	99343	99344	99346	99347	99349	99350	99352	99353
6	99355	99356	99358	99359	99360	99362	99363	99365	99366	99368
7	99369	99370	99372	99373	99374	99376	99377	99379	99380	99381
8	99383	99384	99386	99387	99388	99390	99391	99392	99394	99395
9	99396	99398	99399	99401	99402	99403	99405	99406	99407	99408
23.0	99410	99411	99412	99414	99415	99416	99418	99419	99420	99421
1	99423	99424	99425	99427	99428	99429	99431	99432	99433	99434
2	99436	99437	99438	99439	99440	99442	99443	99445	99446	99447
3	99448	99449	99450	99452	99453	99454	99455	99456	99458	99459
4	99460	99461	99463	99464	99465	99466	99467	99468	99470	99471
5	99472	99473	99474	99476	99477	99478	99479	99480	99481	99483
6	99484	99485	99486	99487	99488	99490	99491	99492	99493	99494
7	99495	99496	99497	99498	99500	99501	99502	99503	99504	99505
8	99506	99507	99508	99509	99511	99512	99513	99514	99515	99516
9	99517	99518	99519	99520	99521	99522	99524	99525	99526	99527
24.0	99528	99529	99530	99531	99532	99533	99534	99535	99536	99537
1	99538	99539	99540	99541	99542	99543	99544	99545	99546	99547
2	99548	99549	99550	99551	99552	99553	99554	99555	99556	99557
3	99558	99559	99560	99561	99562	99563	99564	99565	99566	99567
4	99568	99569	99570	99571	99572	99573	99574	99575	99576	99577
5	99578	99579	99580	99581	99581	99582	99583	99584	99585	99586
6	99587	99588	99589	99590	99591	99592	99593	99593	99594	99595
7	99596	99597	99598	99599	99600	99601	99602	99602	99603	99604
8	99605	99606	99607	99608	99609	99609	99610	99611	99612	99613
9	99614	99615	99615	99616	99617	99618	99619	99620	99621	99621
25.0	99622	99623	99624	99625	99626	99626	99627	99628	99628	99629
1	99630	99631	99632	99633	99634	99635	99636	99636	99637	99638
2	99639	99640	99640	99641	99642	99643	99644	99644	99645	99646
3	99647	99648	99648	99649	99650	99651	99651	99652	99653	99654
4	99655	99655	99656	99657	99658	99659	99659	99660	99661	99661
5	99662	99663	99664	99664	99665	99666	99667	99668	99668	99669
6	99670	99670	99671	99672	99672	99673	99674	99675	99675	99676
7	99677	99678	99678	99679	99680	99681	99681	99682	99683	99683
8	99684	99685	99685	99686	99687	99687	99688	99689	99690	99690
9	99691	99692	99692	99693	99694	99694	99695	99696	99696	99697
26.0	99698	99699	99699	99700	99700	99701	99702	99703	99703	99704
1	99704	99705	99706	99706	99707	99707	99708	99708	99709	99710
2	99711	99712	99712	99713	99714	99714	99715	99716	99716	99717
3	99717	99718	99719	99719	99720	99720	99721	99722	99722	99723
4	99724	99724	99725	99726	99726	99727	99727	99728	99728	99729
5	99730	99730	99731	99731	99732	99733	99733	99734	99734	99735
6	99736	99736	99737	99738	99738	99739	99739	99740	99740	99741
7	99741	99742	99743	99743	99744	99744	99745	99746	99746	99747
8	99747	99748	99749	99749	99750	99750	99751	99751	99752	99752
9	99753	99753	99754	99755	99755	99756	99756	99757	99757	99758
27.0	99759	99759	99759	99760	99760	99761	99761	99762	99762	99763
1	99764	99764	99765	99765	99766	99766	99767	99767	99768	99768
2	99769	99769	99770	99770	99771	99771	99772	99772	99773	99773
3	99774	99774	99775	99775	99776	99776	99777	99777	99778	99778
4	99779	99779	99780	99780	99781	99781	99782	99782	99783	99783
5	99784	99784	99785	99785	99786	99786	99787	99787	99788	99788
6	99789	99789	99789	99790	99790	99791	99791	99792	99792	99793
7	99793	99794	99794	99795	99795	99796	99796	99796	99797	99797
8	99798	99798	99799	99799	99800	99800	99800	99801	99801	99802
9	99802	99803	99803	99804	99804	99805	99805	99805	99806	99806

- Continued -

Table 15.- Values of $1-R^x$ when R = 0.8 - Continued
(All values are decimal fractions)

x	0	1	2	3	4	5	6	7	8	9
28.0	99807	99807	99807	99808	99808	99809	99809	99810	99810	99810
1	99811	99811	99812	99812	99813	99813	99813	99814	99814	99815
2	99815	99816	99816	99816	99817	99817	99817	99818	99818	99819
3	99819	99820	99820	99820	99821	99821	99821	99822	99822	99823
4	99823	99823	99824	99824	99825	99825	99825	99826	99826	99827
5	99827	99827	99828	99828	99829	99829	99829	99830	99830	99830
6	99831	99831	99832	99832	99832	99833	99833	99833	99834	99834
7	99835	99835	99835	99836	99836	99836	99836	99837	99837	99838
8	99838	99839	99839	99839	99840	99840	99840	99841	99841	99841
9	99842	99842	99842	99843	99843	99844	99844	99844	99845	99845
29.0	99845	99846	99846	99846	99847	99847	99847	99848	99848	99848
1	99849	99849	99849	99850	99850	99850	99851	99851	99851	99852
2	99852	99852	99853	99853	99853	99854	99854	99854	99855	99855
3	99855	99856	99856	99856	99857	99857	99857	99858	99858	99858
4	99858	99859	99859	99859	99860	99860	99860	99861	99861	99861
5	99862	99862	99862	99862	99863	99863	99863	99864	99864	99864
6	99865	99865	99865	99866	99866	99866	99866	99867	99867	99867
7	99868	99868	99868	99869	99869	99869	99869	99870	99870	99870
8	99871	99871	99871	99871	99872	99872	99872	99873	99873	99873
9	99873	99874	99874	99874	99875	99875	99875	99875	99876	99876

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